



4



First Year Civil Engineering  
Theory OF Structures (1)

Chapter (8)

CORE METHOD

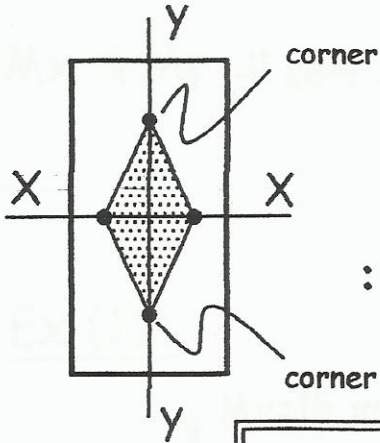


2009-2010



# CORE METHOD

• هي طريقة تستخدم لعمل check على اجهادات ال Normal Stresses من الموضوع السابق



• ال Core هو مساحة وهمية داخل القطاع مكونة من عدة corners

• سوف نستخدم مجموعة قوانين في هذا الدرس و هي :

$$i_x^2 = \frac{I_x}{A}$$

$$i_y^2 = \frac{I_y}{A}$$

$$e_y = \frac{i_x^2}{y_{int}}$$

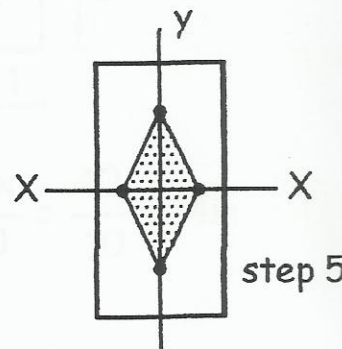
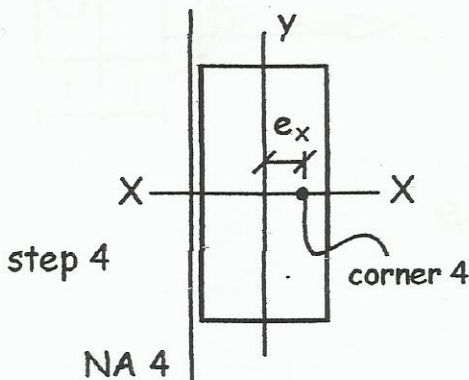
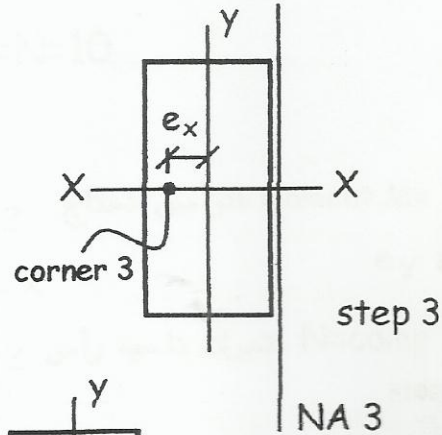
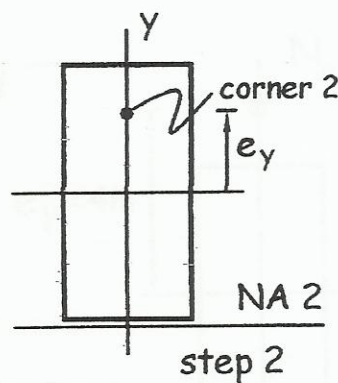
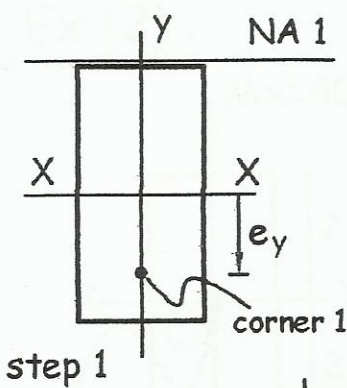
$$e_x = \frac{i_y^2}{x_{int}}$$

• خطوات الحل :

1 - يتم حساب ال  $i_x^2, i_y^2, A, I_x, I_y$  properties of area

2 - يتم فرض مجموعة Neutral Axes (N.A) بحيث تماس القطاع

3 - عند فرض أي Neutral Axes (N.A) فانه يتواجد corner في الناحية المقابلة له على بعد فقى أو رأسى  $e_x, e_y$  بمعنى

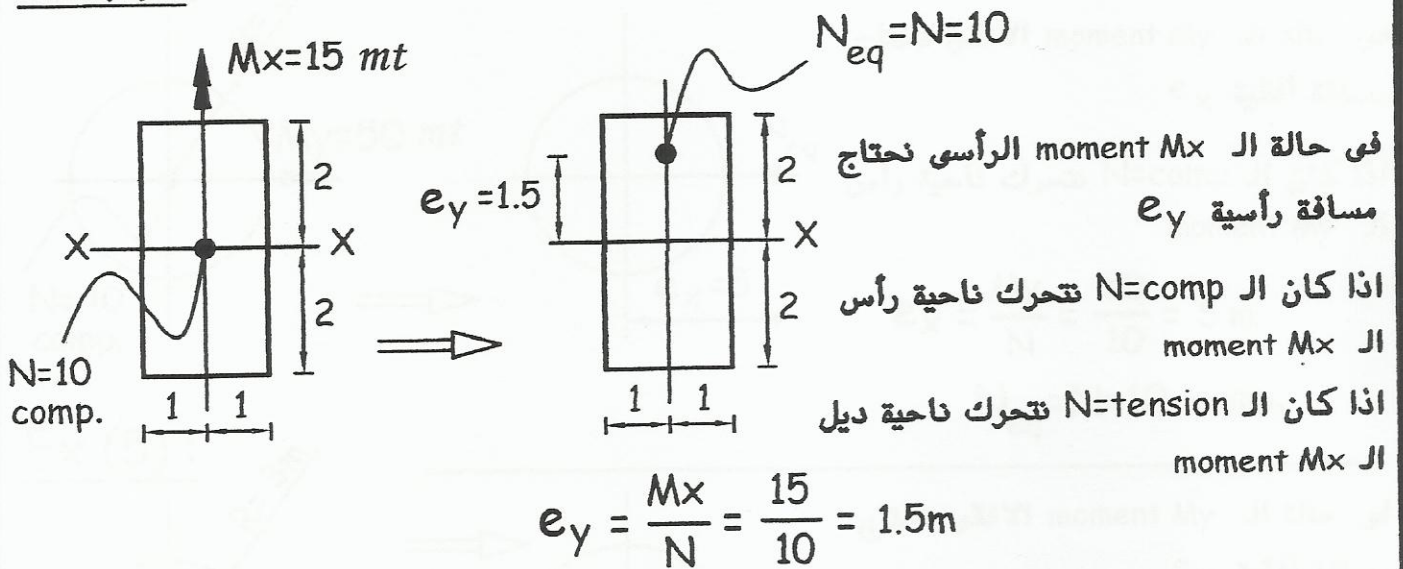




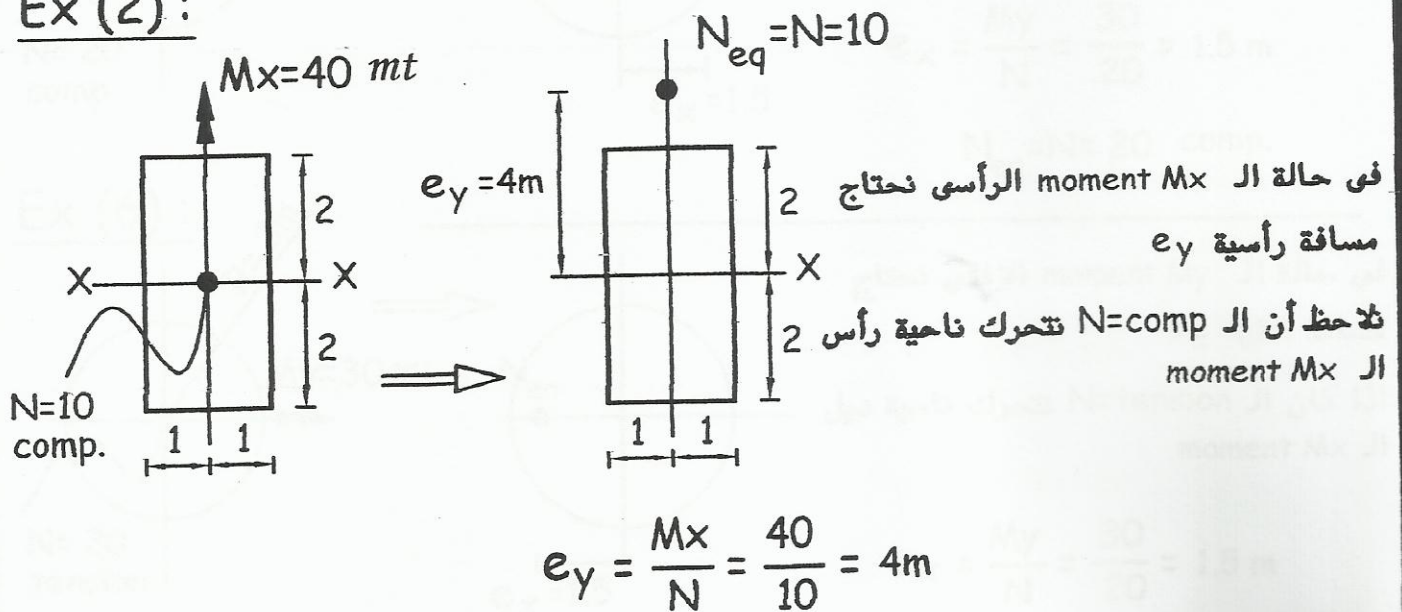
## • تابع خطوات الحل :

4 - بعد رسم ال Core يتم تحديد مكان نقطة ال  $N_{eq}$  equivalent normal  
و هي قوة لا تمر بال C.g و تساوى عدديا قيمة ال  $N$  و تعتبر بديل لـ  $M_x$  &  $M_y$   
مع ملاحظة توقيع ال  $N_{eq}$  مع اتجاه ال  $M_x$  &  $M_y$

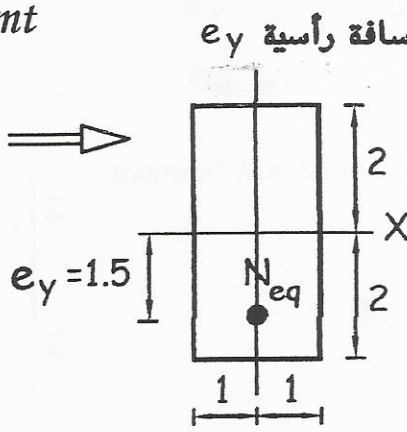
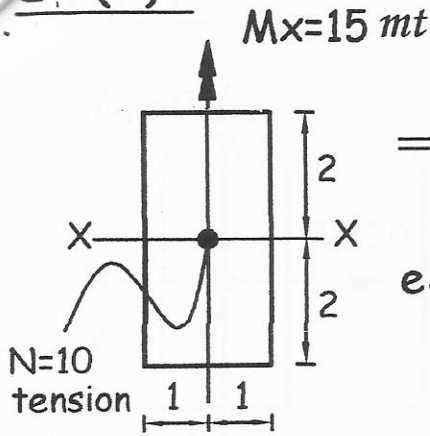
### Ex (1) :



### Ex (2) :



Ex (3) :

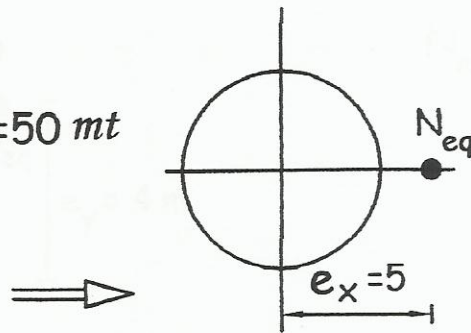
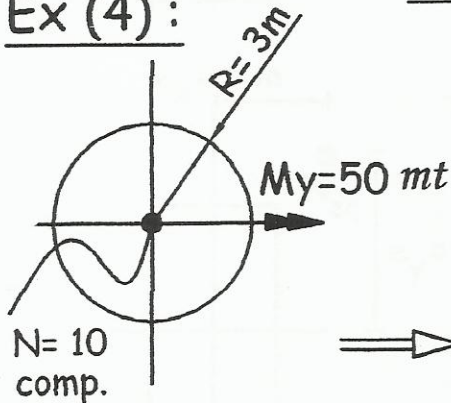


في حالة ال moment  $M_x$  الرأسى نحتاج مسافة رأسية  $e_y$   
إذا كان ال  $N = \text{tension}$  تتحرك ناحية ديل  
ال moment  $M_x$

$$e_y = \frac{M_x}{N} = \frac{15}{10} = 1.5 \text{ m}$$

$$N_{eq} = N = 10 \text{ tension}$$

Ex (4) :



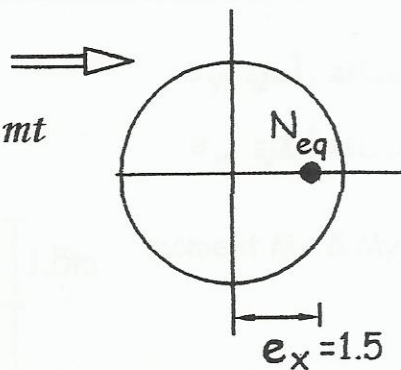
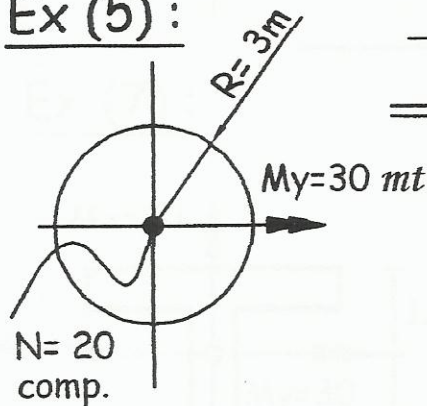
في حالة ال moment  $M_y$  الافقى نحتاج  
مسافة أفقية  $e_x$

إذا كان ال  $N = \text{comp}$  تتحرك ناحية رأس  
ال moment  $M_y$

$$e_x = \frac{M_y}{N} = \frac{50}{10} = 5 \text{ m}$$

$$N_{eq} = N = 10 \text{ comp.}$$

Ex (5) :



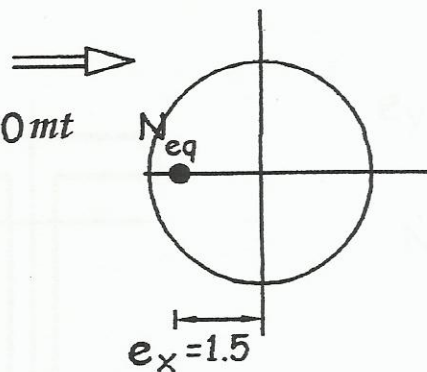
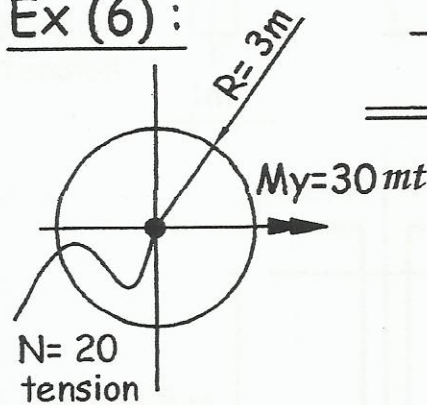
في حالة ال moment  $M_y$  الافقى نحتاج  
مسافة أفقية  $e_x$

إذا كان ال  $N = \text{comp}$  تتحرك ناحية رأس  
ال moment  $M_y$

$$e_x = \frac{M_y}{N} = \frac{30}{20} = 1.5 \text{ m}$$

$$N_{eq} = N = 20 \text{ comp.}$$

Ex (6) :



في حالة ال moment  $M_y$  الافقى نحتاج  
مسافة أفقية  $e_x$

إذا كان ال  $N = \text{tension}$  تتحرك ناحية ديل  
ال moment  $M_x$

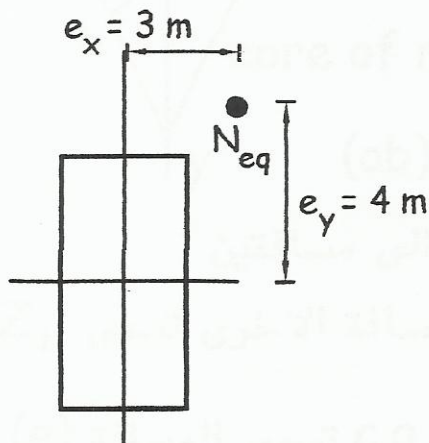
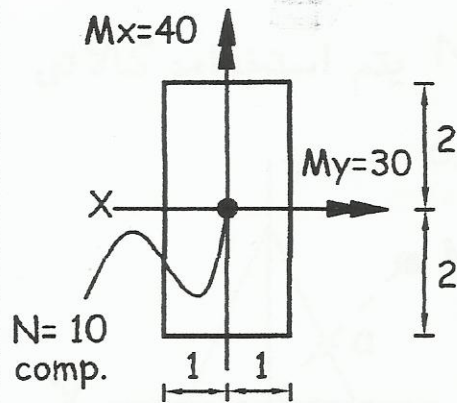
$$e_x = \frac{M_y}{N} = \frac{30}{20} = 1.5 \text{ m}$$

$$N_{eq} = N = 20 \text{ tension}$$





### Ex (6) :



في حالة ال moment الرأسى نحتاج مسافة رأسية  $e_y$

و في حالة ال moment الافقى نحتاج مسافة أفقية  $e_x$

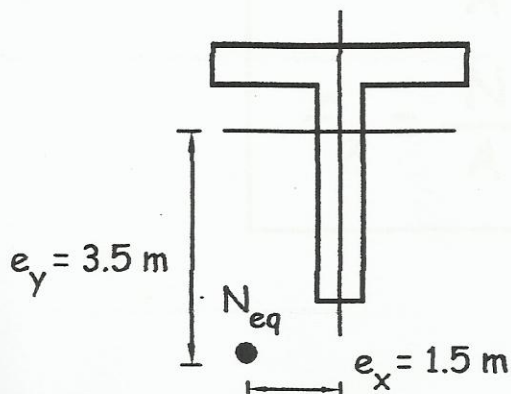
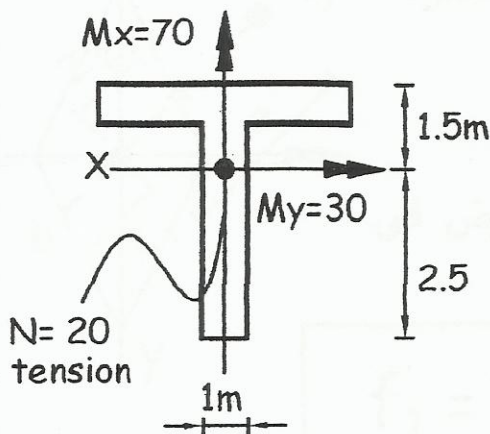
إذا كان ال  $N = \text{comp}$  تتحرك ناحية رأس ال moment  $M_x$  &  $M_y$

$$e_x = \frac{M_y}{N} = \frac{30}{10} = 3 \text{ m}$$

$$e_y = \frac{M_x}{N} = \frac{40}{10} = 4 \text{ m}$$

$$N_{eq} = N = 10 \text{ comp.}$$

### Ex (7) :



في حالة ال moment الرأسى نحتاج مسافة رأسية  $e_y$

و في حالة ال moment الافقى نحتاج مسافة أفقية  $e_x$

إذا كان ال  $N = \text{tension}$  تتحرك ناحية ديل ال moment  $M_x$  &  $M_y$

$$e_x = \frac{M_y}{N} = \frac{30}{20} = 1.5 \text{ m}$$

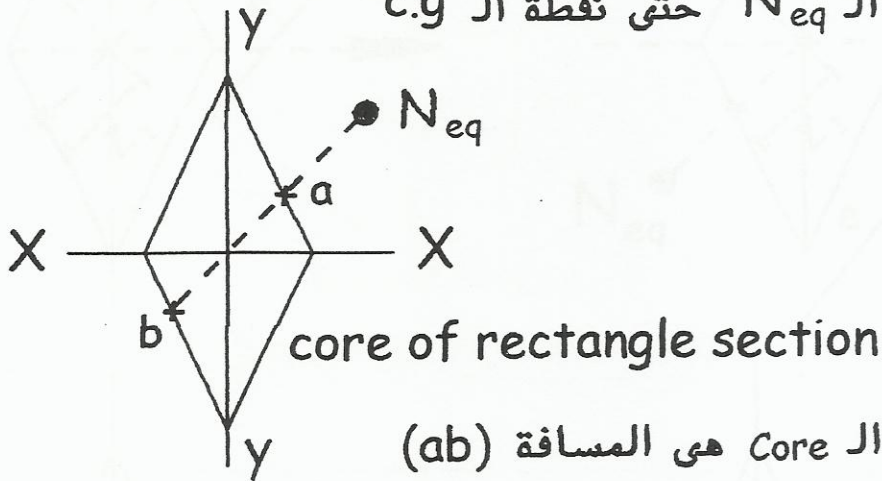
$$e_y = \frac{M_x}{N} = \frac{70}{20} = 3.5 \text{ m}$$

$$N_{eq} = N = 20 \text{ tension}$$

## تابع خطوات الحل :

5 - بعد رسم ال Core و تحديد مكان نقطة ال  $N_{eq}$  يتم استخدامه كالآتى

• نرسم خط من نقطة ال  $N_{eq}$  حتى نقطة ال c.g

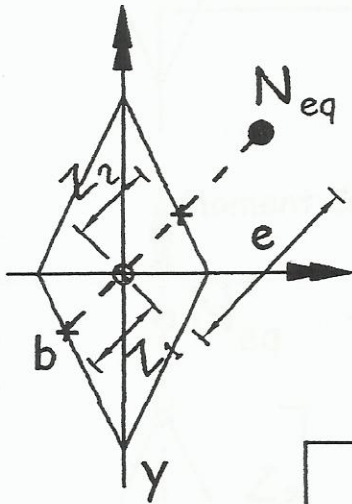


• مسافة التقاطع مع ال Core هي المسافة (ab)

• نقطة ال c.g تقوم بتقسيم المسافة (ab) الى مسافتين

المسافة ناحية Moment Comp. تسمى  $Z_2$  و المسافة الاخرى تسمى  $Z_1$

• المسافة مباشرة من ال  $N_{eq}$  حتى نقطة ال c.g تسمى المسافة (e)



• يتم قياس المسافات (e) (Z<sub>1</sub>) (Z<sub>2</sub>) بالمسطرة

و عمل check stresses (f<sub>1</sub>) (f<sub>2</sub>) بالتعويض فى

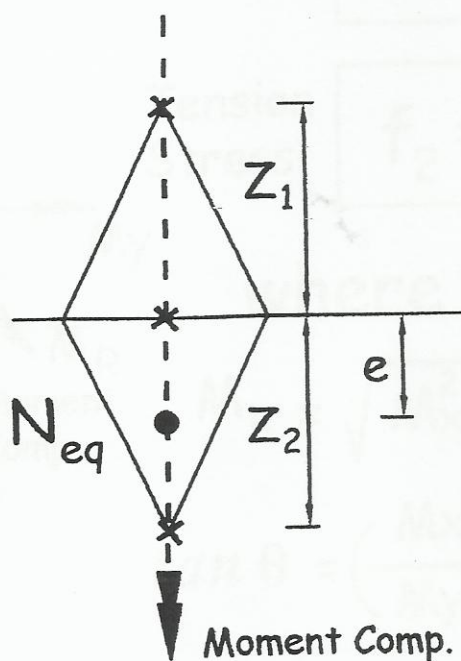
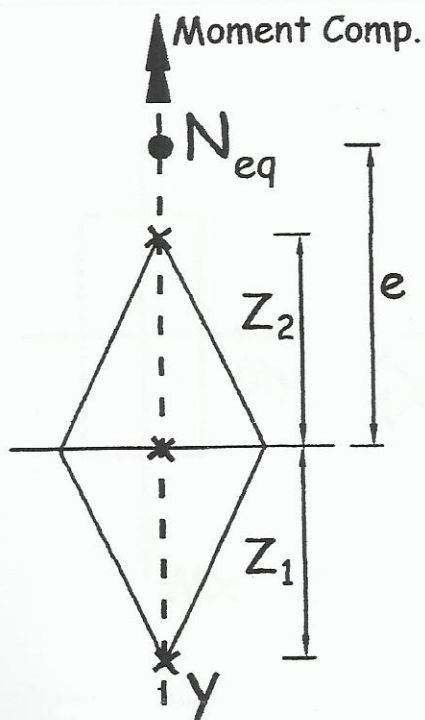
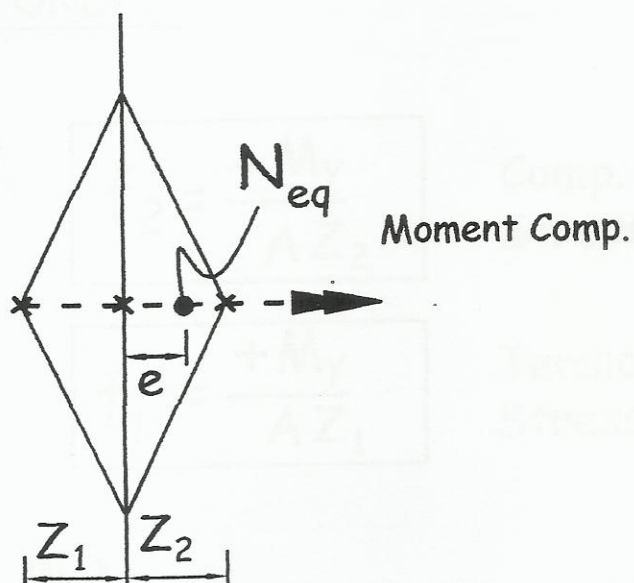
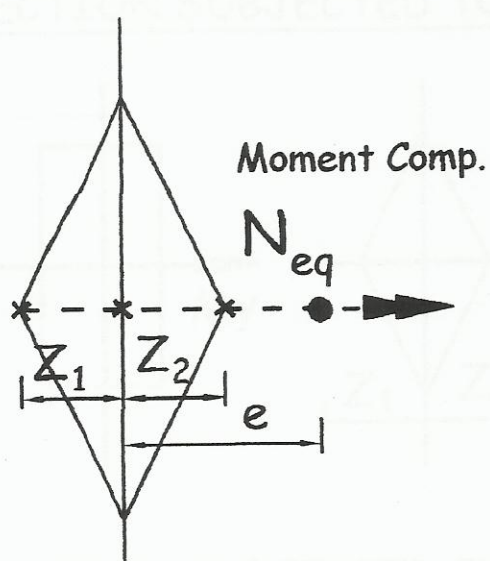
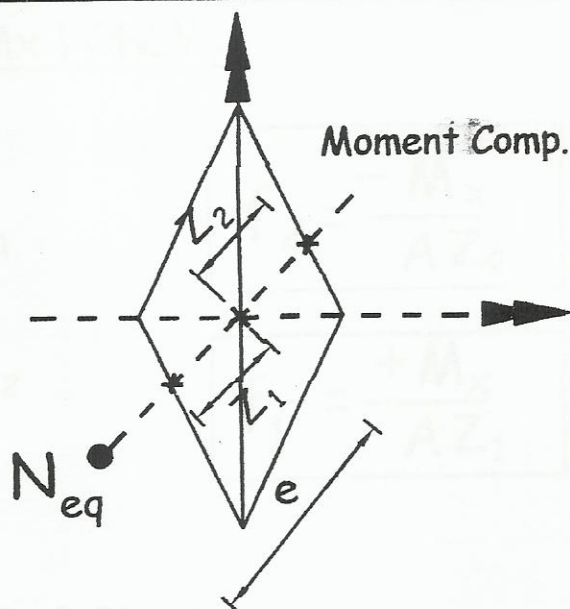
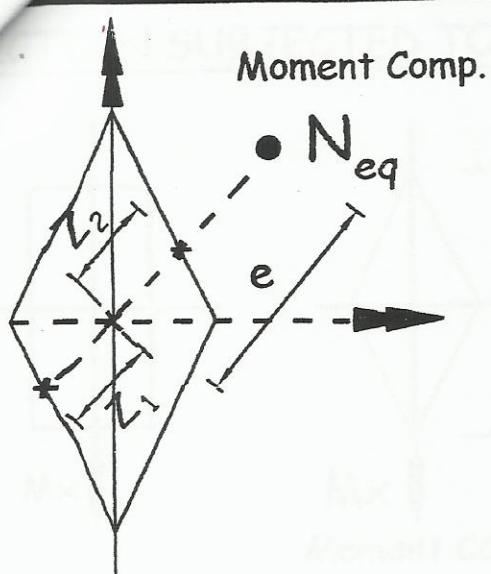
القوانين الآتية

$$f_1 = \frac{N}{A} \left[ \frac{Z_1 + e}{Z_1} \right]$$

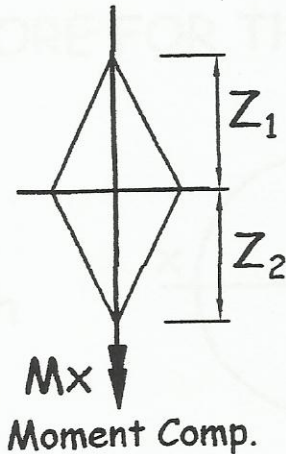
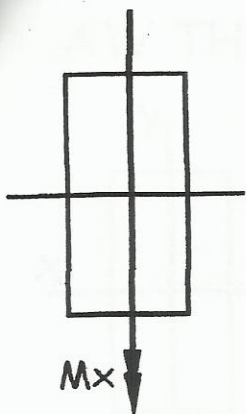
$$f_2 = \frac{N}{A} \left[ \frac{Z_2 - e}{Z_2} \right]$$

حفظ





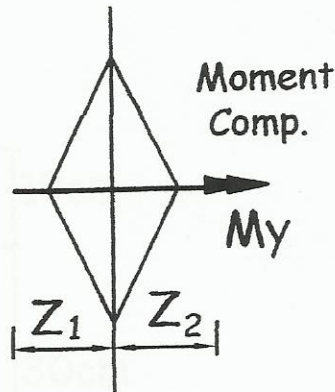
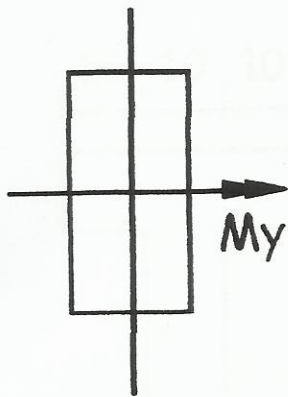
### SECTION SUBJECTED TO ( $M_x$ ) ONLY :



$$f_2 = -\frac{M_x}{AZ_2} \quad \text{Comp. Stress}$$

$$f_1 = +\frac{M_x}{AZ_1} \quad \text{Tension Stress}$$

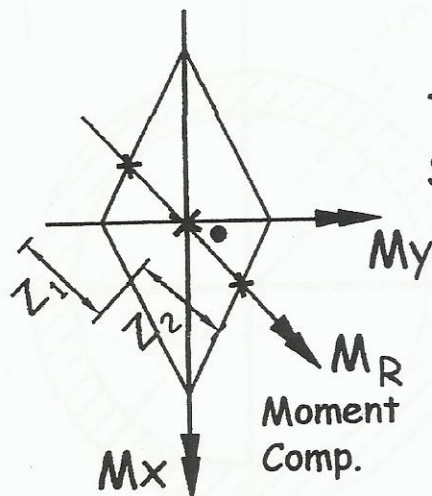
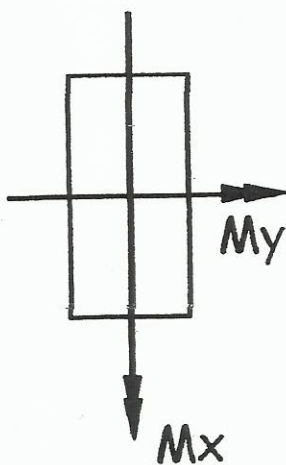
### SECTION SUBJECTED TO ( $M_y$ ) ONLY :



$$f_2 = -\frac{M_y}{AZ_2} \quad \text{Comp. Stress}$$

$$f_1 = +\frac{M_y}{AZ_1} \quad \text{Tension Stress}$$

### SECTION SUBJECTED TO ( $M_x, M_y$ ) :



Comp. Stress

$$f_1 = -\frac{M_R}{AZ_1}$$

Tension Stress

$$f_2 = +\frac{M_R}{AZ_2}$$

where :

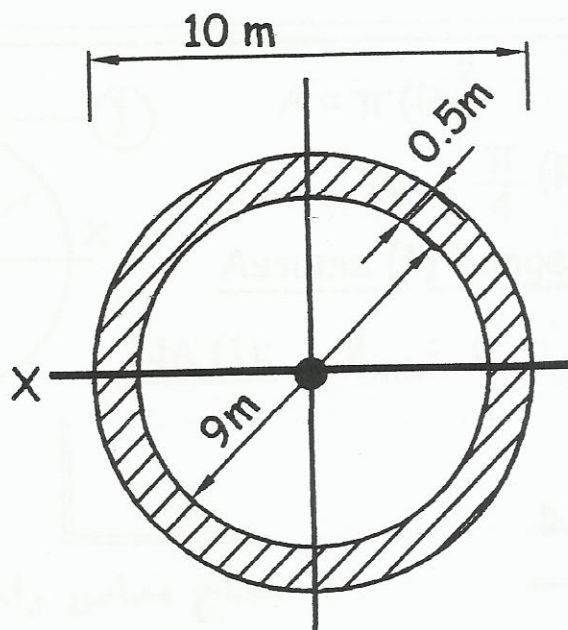
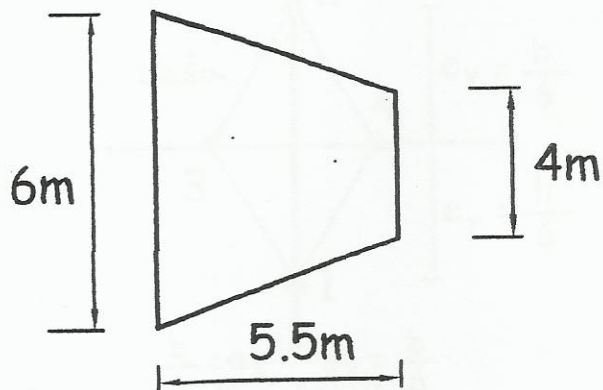
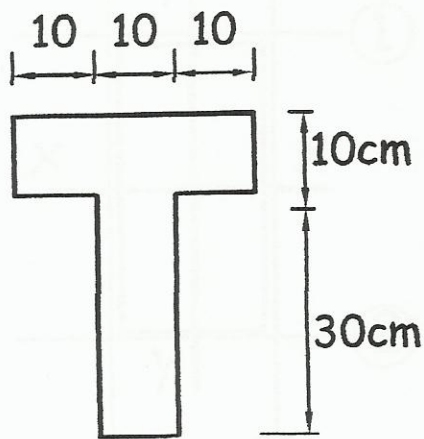
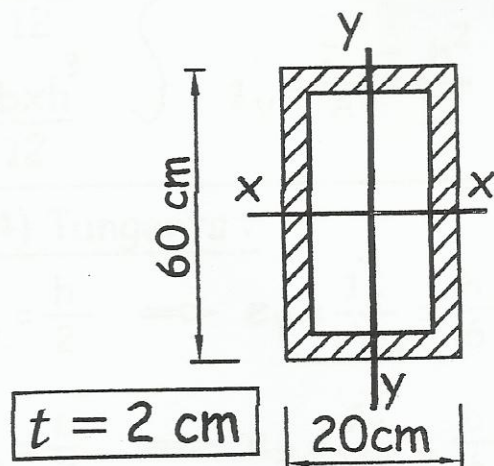
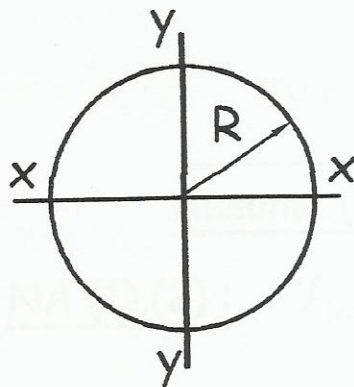
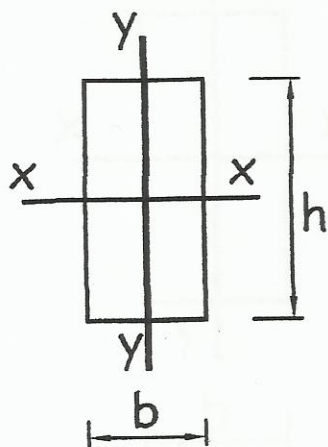
$$M_R = \sqrt{M_x^2 + M_y^2}$$

$$\tan \theta = \left( \frac{M_x}{M_y} \right)$$

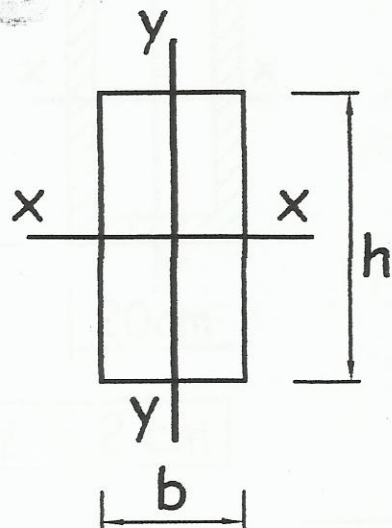


# PROBLEM(1):

DRAW THE CORE FOR THE SHOWN SECTIONS ?



# SOLUTION :

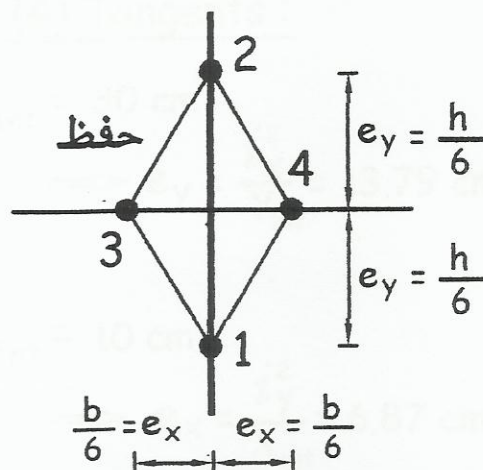
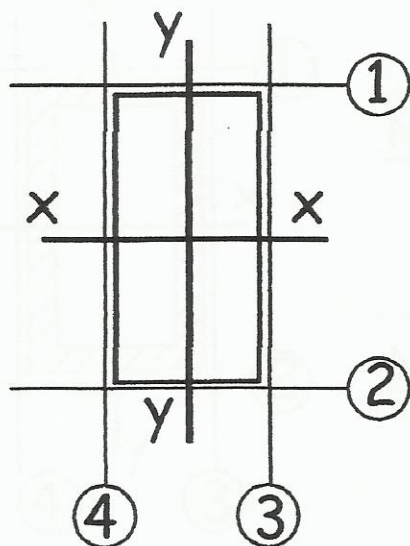


$$\begin{aligned} A &= b \times h \\ I_x &= \frac{b x h^3}{12} \\ I_y &= \frac{b x h^3}{12} \end{aligned} \quad \left. \begin{aligned} i_x^2 &= \frac{I_x}{A} = \frac{h^2}{12} \\ i_y^2 &= \frac{I_y}{A} = \frac{b^2}{12} \end{aligned} \right\}$$

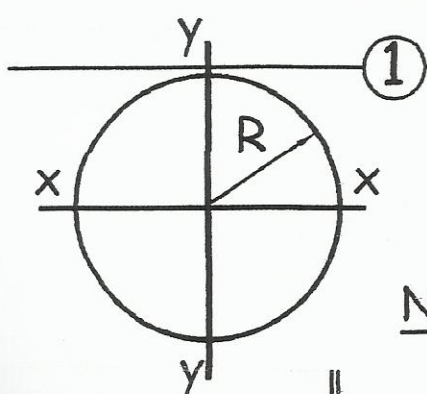
Assume (4) Tangents :

NA (1),(2) :  $Y_{int.} = \frac{h}{2} \Rightarrow e_y = \frac{i_x^2}{Y_{int.}} = \frac{h}{6}$

NA (3),(4) :  $X_{int.} = \frac{b}{2} \Rightarrow e_x = \frac{i_y^2}{X_{int.}} = \frac{b}{6}$



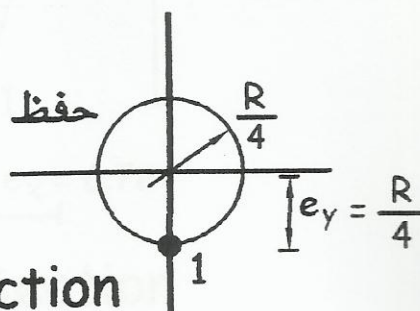
Core of Section



$$\begin{aligned} A &= \pi (R)^2 \\ I_x &= I_y = \frac{\pi}{4} (R)^4 \end{aligned} \quad \left. \begin{aligned} i_x^2 &= i_y^2 = \frac{R^2}{4} \end{aligned} \right\}$$

Assume (1) Tangent :

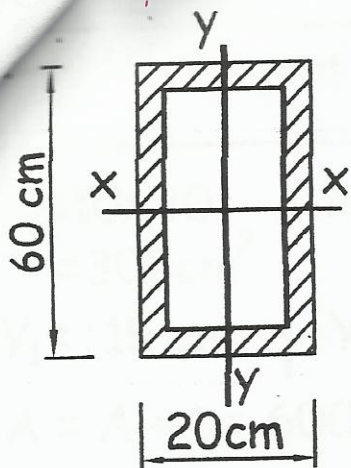
NA (1) :  $Y_{int.} = R \Rightarrow e_y = \frac{i_x^2}{Y_{int.}} = \frac{R}{4}$



نحتاج مماس واحد لان الدائرة متماثلة حول جميع المحاور

Core of Section





$$t = 2 \text{ cm}$$

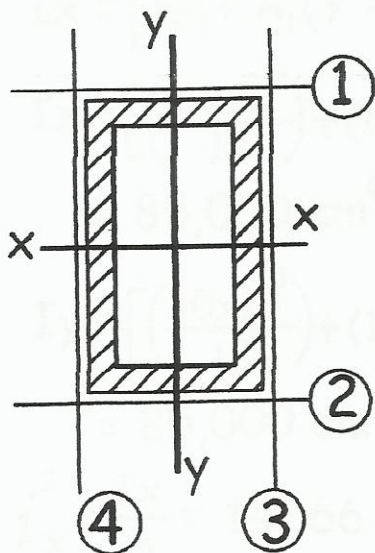
$$A = 20 \times 60 - 16 \times 56 = 304 \text{ cm}^2$$

$$I_x = \frac{20 \times 60^3}{12} - \frac{16 \times 56^3}{12} = 125\,845 \text{ cm}^4$$

$$I_y = \frac{60 \times 20^3}{12} - \frac{56 \times 16^3}{12} = 20\,885 \text{ cm}^4$$

$$i_x^2 = \frac{I_x}{A} = 413.96 \text{ cm}^2$$

$$i_y^2 = \frac{I_y}{A} = 68.7 \text{ cm}^2$$



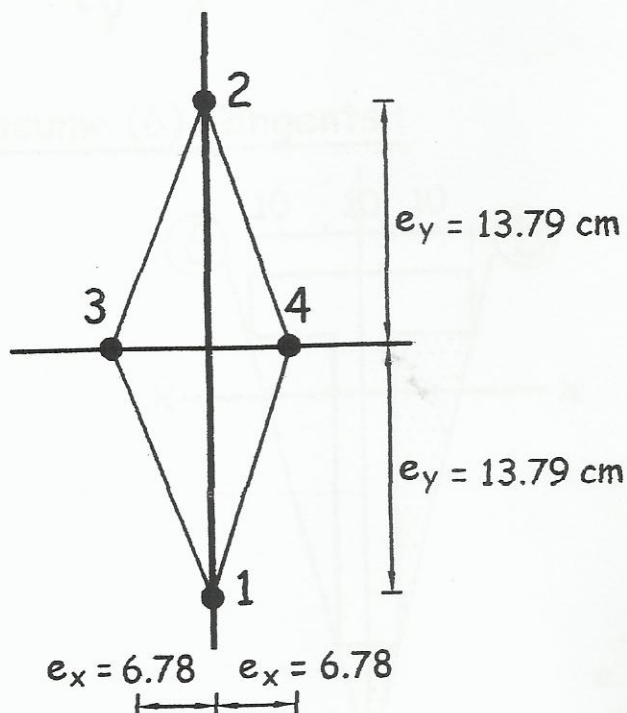
Assume (4) Tangents :

$$\text{NA (1),(2): } Y_{\text{int.}} = 30 \text{ cm}$$

$$\Rightarrow e_y = \frac{i_x^2}{Y_{\text{int}}} = 13.79 \text{ cm}$$

$$\text{NA (3),(4): } X_{\text{int.}} = 10 \text{ cm}$$

$$\Rightarrow e_x = \frac{i_y^2}{X_{\text{int}}} = 6.87 \text{ cm}$$



Core of Section

في حالة عدم وجود محور (X) فاننا نحدد المسافة  $\bar{Y} = ?$

$$A_1 = 10 \times 30 = 300 \text{ cm}^2 \quad A_2 = 10 \times 30 = 300 \text{ cm}^2$$

$$Y_1 = 15 \text{ cm} \quad Y_2 = 35 \text{ cm}$$

$$A = A_1 + A_2 = 600 \text{ cm}^2$$

$$\bar{Y} = \frac{\sum AY}{\sum A} = \frac{A_1 Y_1 + A_2 Y_2}{A_1 + A_2} = 25 \text{ cm}$$

$$I_x = [I_{x_1} + A_1 (\bar{Y} - Y_1)^2] + [I_{x_2} + A_2 (\bar{Y} - Y_2)^2]$$

$$I_x = \left[ \left( \frac{10 \times 30^3}{12} \right) + (10 \times 30)(25 - 15)^2 \right] + \left[ \left( \frac{30 \times 10^3}{12} \right) + (10 \times 30)(25 - 35)^2 \right]$$

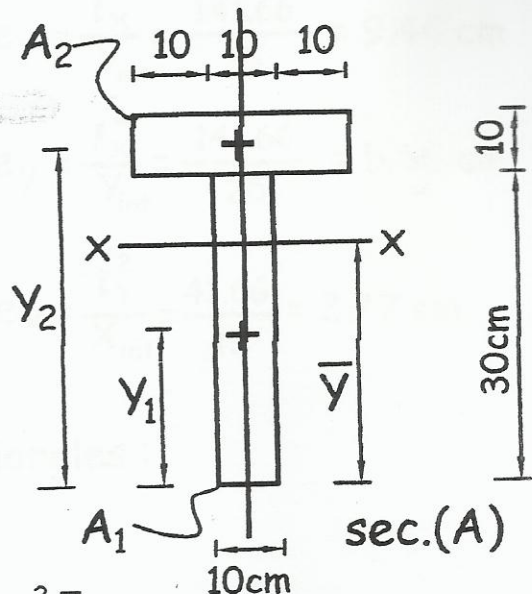
$$= 85,000 \text{ cm}^4$$

$$I_y = \left[ \left( \frac{30 \times 10^3}{12} \right) + (10 \times 30)(0.0)^2 \right] + \left[ \left( \frac{10 \times 30^3}{12} \right) + (10 \times 30)(0.0)^2 \right]$$

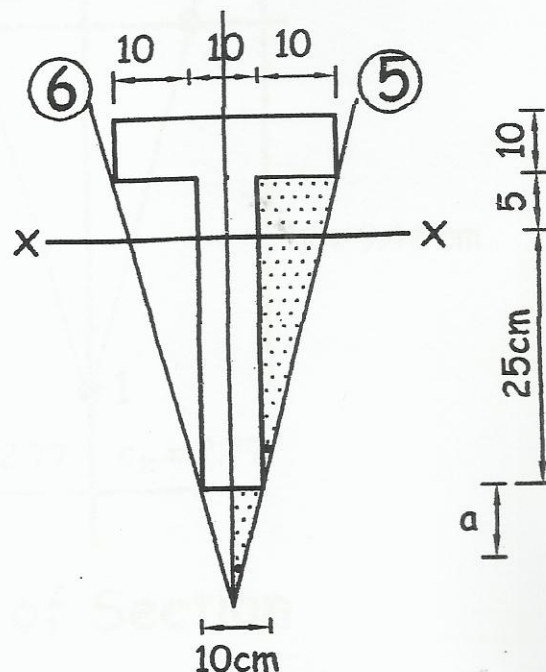
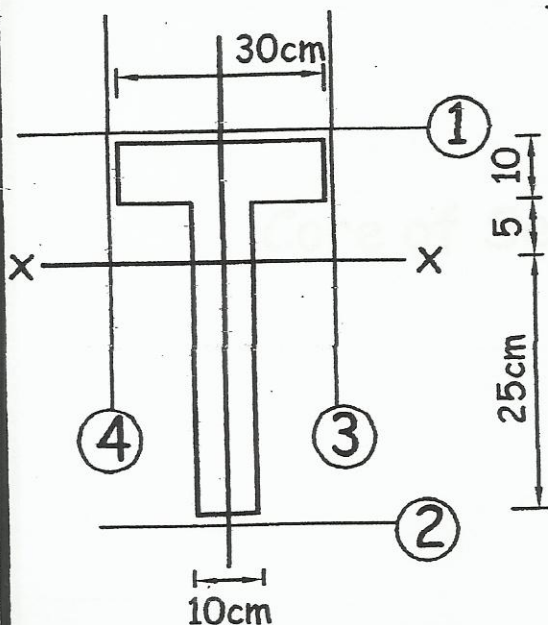
$$= 25,000 \text{ cm}^4$$

$$i_x^2 = \frac{I_x}{A} = 141.66 \text{ cm}^2$$

$$i_y^2 = \frac{I_y}{A} = 41.66 \text{ cm}^2$$



Assume (6) Tangents :





NA (1):  $Y_{int.} = 15 \text{ cm} \Rightarrow e_y = \frac{i_x^2}{Y_{int.}} = \frac{141.66}{15} = 9.44 \text{ cm}$

NA (2):  $Y_{int.} = 25 \text{ cm} \Rightarrow e_y = \frac{i_x^2}{Y_{int.}} = \frac{141.66}{25} = 5.66 \text{ cm}$

NA (3),(4):  $X_{int.} = 10 \text{ cm} \Rightarrow e_x = \frac{i_y^2}{X_{int.}} = \frac{41.66}{15} = 2.77 \text{ cm}$

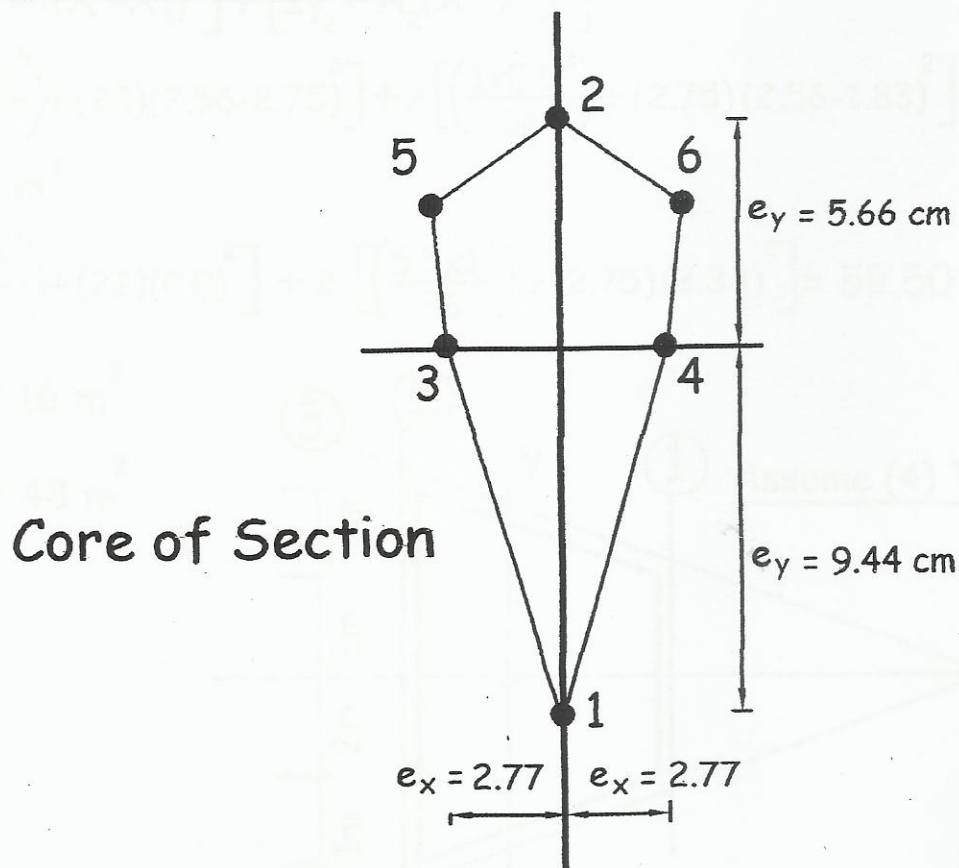
NA (5): by similarity of hatched triangles :

$\frac{5}{a} = \frac{10}{30} = \frac{X_{int.}}{Y_{int.}} \Rightarrow a = 15 \text{ cm}$

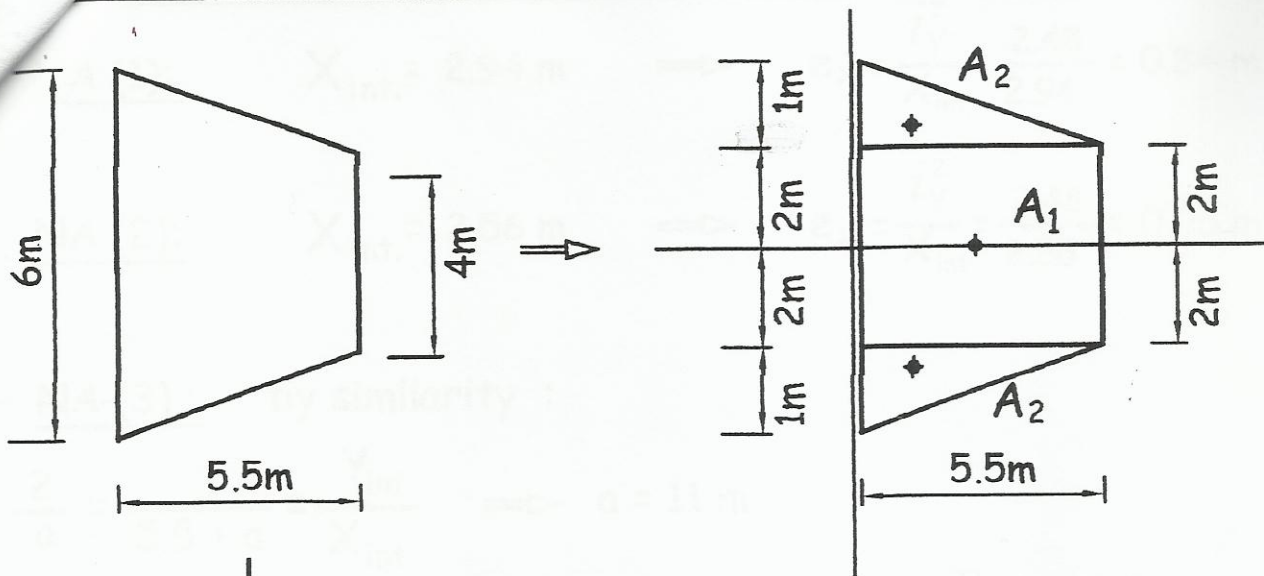
$\Rightarrow Y_{int.} = \bar{Y} + a = 25 + 15 = 40 \text{ cm} \Rightarrow e_y = \frac{i_x^2}{Y_{int.}} = \frac{141.66}{40} = 3.54 \text{ cm}$

$\Rightarrow X_{int.} = 13.33 \text{ cm} \Rightarrow e_x = \frac{i_y^2}{X_{int.}} = \frac{41.66}{13.33} = 3.12 \text{ cm}$

NA (5) & NA (6) are the same



Core of Section



$$A_1 = 4 \times 5.5 = 22 \text{ m}^2$$

$$A_2 = 0.5 \times 1 \times 5.5 = 2.75 \text{ m}^2$$

$$X_1 = 2.75$$

$$X_2 = 1.83$$

$$A = A_1 + 2A_2 = 27.5 \text{ m}^2$$

$$\bar{X} = \frac{\sum AX}{\sum A} = \frac{A_1 x_1 + 2A_2 x_2}{A_1 + 2A_2} = 2.566 \text{ m}$$

في حالة عدم وجود محور (Y) فاننا نحسب  
المسافة  $\bar{X} = ?$

$$I_y = [I_{y_1} + A_1(\bar{X} - X_1)^2] + [I_{y_2} + A_2(\bar{X} - X_2)^2]$$

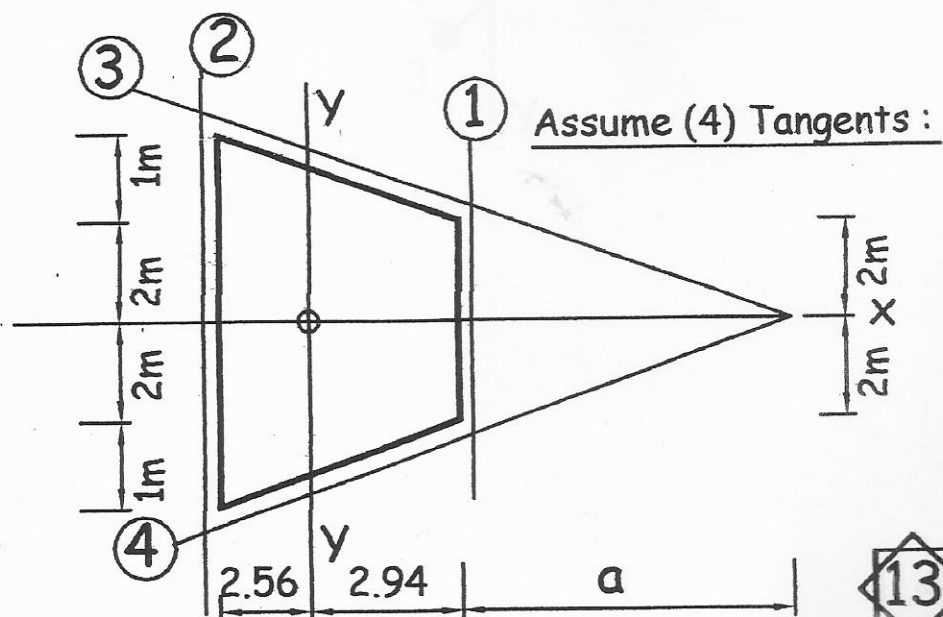
$$I_y = \left[ \left( \frac{4 \times 5.5^3}{12} \right) + (22)(2.56 - 2.75)^2 \right] + 2 \left[ \left( \frac{1 \times 5.5^3}{36} \right) + (2.75)(2.56 - 1.83)^2 \right]$$

$$= 68.40 \text{ m}^4$$

$$I_x = \left[ \left( \frac{5.5 \times 4^3}{12} \right) + (22)(0.0)^2 \right] + 2 \left[ \left( \frac{5.5 \times 1^3}{36} \right) + (2.75)(2.33)^2 \right] = 59.50 \text{ m}^4$$

$$i_x^2 = \frac{I_x}{A} = 2.16 \text{ m}^2$$

$$i_y^2 = \frac{I_y}{A} = 2.48 \text{ m}^2$$





NA (1):  $X_{int.} = 2.94 \text{ m} \Rightarrow e_x = \frac{i_y^2}{X_{int.}} = \frac{2.48}{2.94} = 0.84 \text{ m}$

NA (2):  $X_{int.} = 2.56 \text{ m} \Rightarrow e_x = \frac{i_y^2}{X_{int.}} = \frac{2.48}{2.56} = 0.96 \text{ m}$

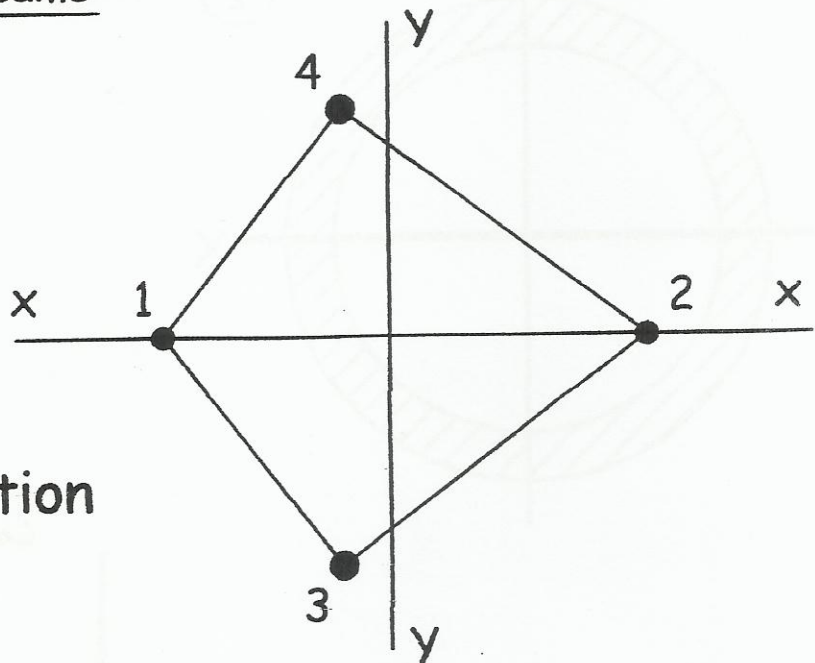
NA (3): by similarity :

$$\frac{2}{a} = \frac{3}{5.5 + a} = \frac{y_{int.}}{X_{int.}} \Rightarrow a = 11 \text{ m}$$

$$\Rightarrow X_{int.} = 2.94 + a = 2.94 + 11 = 13.94 \text{ m} \Rightarrow e_y = \frac{i_x^2}{y_{int.}} = \frac{2.16}{2.53} = 0.853 \text{ m}$$

$$\Rightarrow X_{int.} = 2.53 \text{ m} \Rightarrow e_x = \frac{i_y^2}{X_{int.}} = \frac{2.48}{13.94} = 0.178 \text{ m}$$

NA (3) & NA (4) are the same



Core of Section

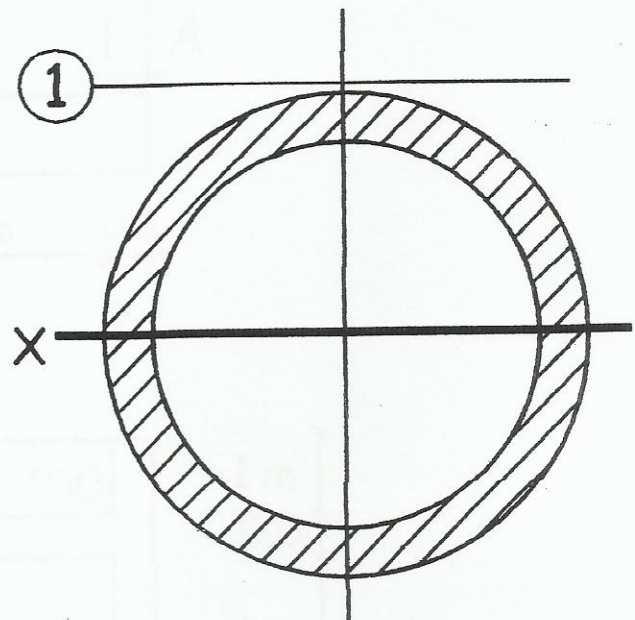
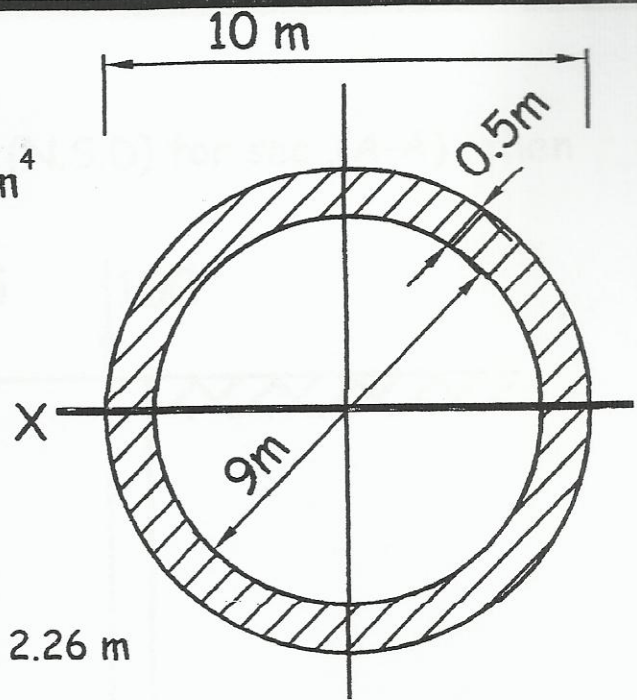
$$A = \frac{\pi}{4}[(10^2 - 9^2)] = 14.92 \text{ m}^2$$

$$I_y = I_x = \frac{\pi}{64}[(10^4 - 9^4)] = 168.81 \text{ m}^4$$

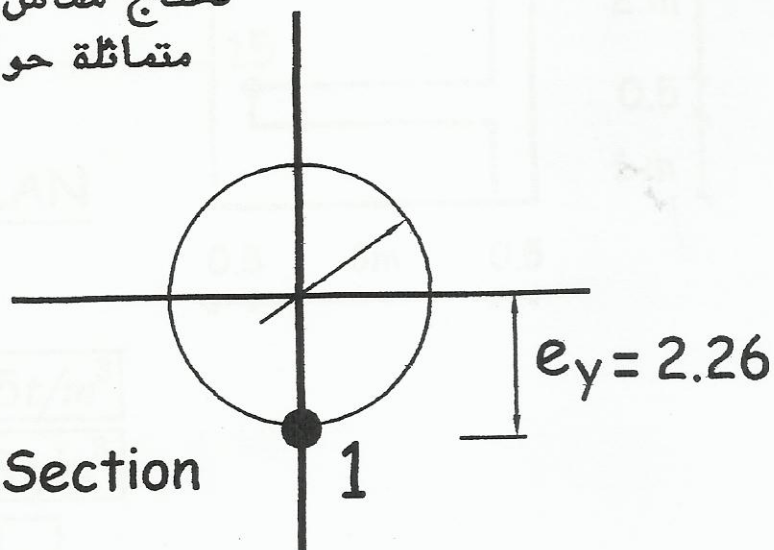
$$i_x^2 = i_y^2 = \frac{I_x}{A} = 11.314 \text{ m}^2$$

NA (1):

$$y_{\text{int.}} = 5 \text{ m} \Rightarrow e_y = \frac{i_x^2}{y_{\text{int}}} = \frac{11.314}{5} = 2.26 \text{ m}$$



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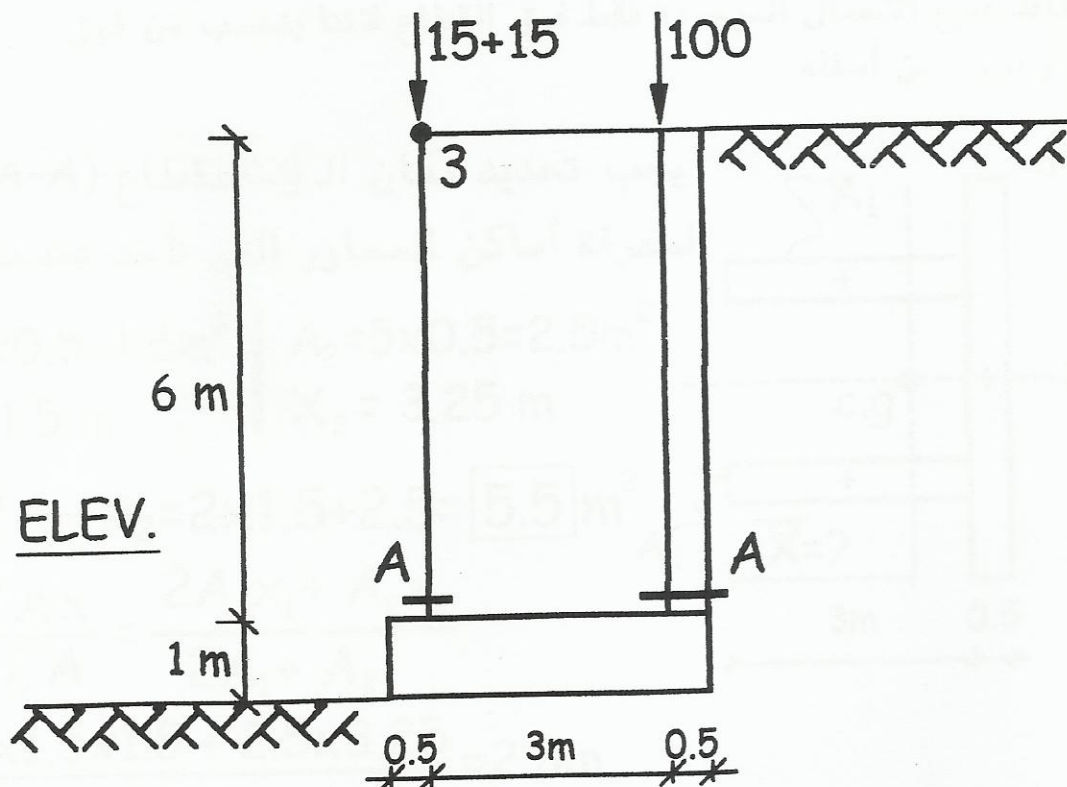


Core of Section

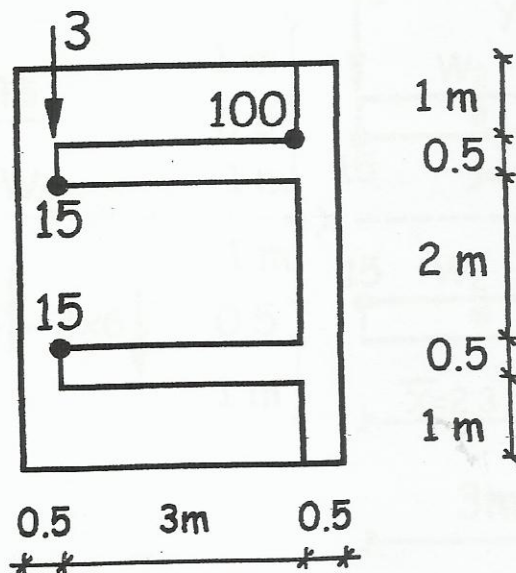


## PROBLEM(2):

Draw Normal Stress Distribution (N.S.D) for sec .(A-A) , then check by core method ?



PLAN



where:

$$\gamma_{R.C} = 2.5 t/m^3$$

$$\gamma_{soil} = 1.8 t/m^3$$

$$K_{soil} = \frac{1}{3}$$

for SEC. (A-A):

- يتم رسم شكل Sec(A) فى ورقة الاجابة و غالبا ما نحصل عليه من ال plan
- لا داعى لرسم ال Elevation فى ورقة الاجابة لتوفير الوقت
- يتم اسقاط جميع الاحمال الموجودة فقط فوق القطاع لاننا بنحسب من فوق القطاع و ليس من أسفله

يجب تحديد مكان ال c.g للقطاع (A-A) و ذلك لمعرفة أماكن المحاور التى نأخذ عندها العزوم

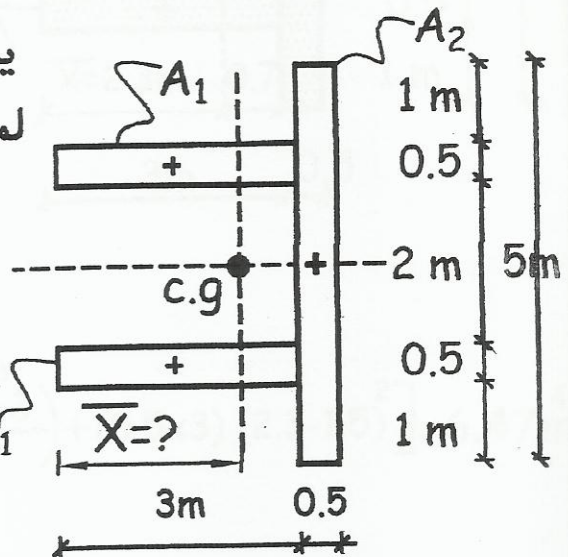
$$A_1 = 3 \times 0.5 = 1.5 \text{ m}^2 \quad | \quad A_2 = 5 \times 0.5 = 2.5 \text{ m}^2$$

$$X_1 = 1.5 \text{ m} \quad | \quad X_2 = 3.25 \text{ m}$$

$$A = 2A_1 + A_2 = 2 \times 1.5 + 2.5 = 5.5 \text{ m}^2$$

$$\bar{X} = \frac{\sum AX}{\sum A} = \frac{2A_1X_1 + A_2X_2}{2A_1 + A_2}$$

$$\bar{X} = \frac{2 \times 1.5 \times 1.5 + 2.5 \times 3.25}{5.5} = 2.3 \text{ m}$$



## 1-Straining actions

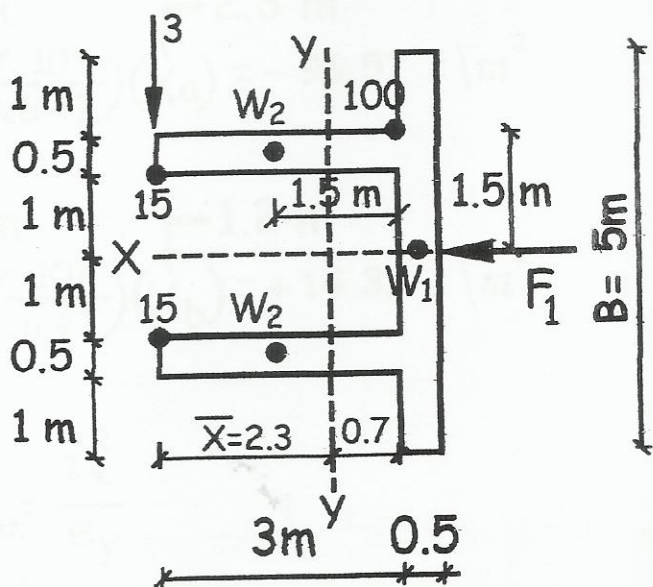
$$N = 15 + 15 + 100 + W_1 + W_2 + W_2 = 212.5 \text{ Comp.}$$

$$M_x = 15 \times 1 \uparrow - 15 \times 1 \downarrow + 100 \times 1.5 \uparrow - 3 \times 6 \downarrow + W_2 \times 1.5 \uparrow - W_2 \times 1.5 \downarrow$$

$$M_x = 132 \uparrow \text{ mt}$$

$$M_y = (15 + 15) \times 2.3 + 2 \times F_1 - 100 \times 0.7 + 2W_2 \times (1.5 - 0.7) - W_1 \times 0.95$$

$$M_y = 107 \text{ mt}$$



SEC(A-A)



## Properties of Area:

$$A = 2A_1 + A_2 = 2 \times 1.5 + 2.5 = 5.5 \text{ m}^2$$

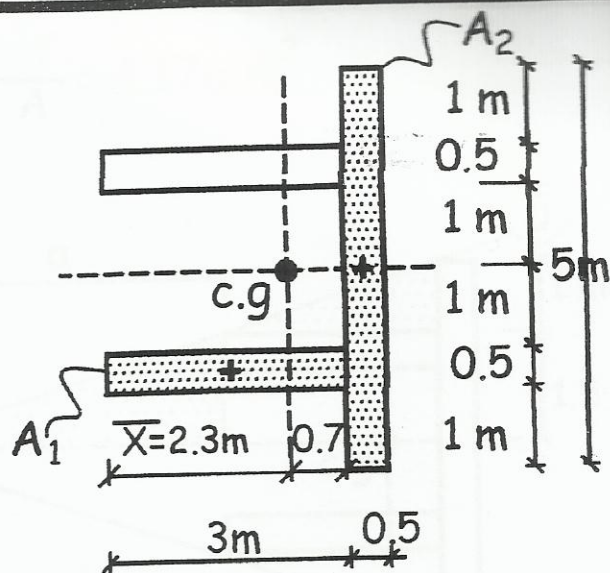
$$I_x = \sum [I_x + A (\Delta Y)^2]$$

$$I_x = \left[ \left( \frac{0.5 \times 5^3}{12} \right) + (0.5 \times 5) (0.0)^2 \right] + 2 \left[ \left( \frac{3 \times 0.5^3}{12} \right) + (0.5 \times 3) (1.25)^2 \right]$$

$$I_x = 9.958 \text{ m}^4$$

$$I_y = \sum [I_y + A (\bar{X} - X)^2]$$

$$I_y = \left[ \left( \frac{5 \times 0.5^3}{12} \right) + (0.5 \times 5) (2.3 - 3.25)^2 \right] + 2 \left[ \left( \frac{0.5 \times 3^3}{12} \right) + (0.5 \times 3) (2.3 - 1.5)^2 \right] = 6.47 \text{ m}^4$$



## 3-DRAW NORMAL STRESS:

$$f = \pm \left( \frac{N}{A} \right) \pm \left( \frac{M_x}{I_x} \right) (y) \pm \left( \frac{M_y}{I_y} \right) (x)$$

$$\therefore f_a = \left( \frac{-212.5}{5.5} \right) - \left( \frac{132}{9.95} \right) (\overset{\downarrow 1.5 \text{ m}}{y_a}) - \left( \frac{107}{6.47} \right) (\overset{\downarrow 2.3 \text{ m}}{x_a}) = -96.57 \text{ t/m}^2$$

$$\therefore f_b = \left( \frac{-212.5}{5.5} \right) - \left( \frac{132}{9.95} \right) (\overset{\downarrow 2.5 \text{ m}}{y_b}) - \left( \frac{107}{6.47} \right) (\overset{\downarrow 1.2 \text{ m}}{x_b}) = +14.37 \text{ t/m}^2$$

$$X_{int.} = \frac{i_y^2}{e_x}$$

$$i_y^2 = \frac{I_y}{A} = \frac{6.47}{5.5} = 1.17 \text{ m}^2$$

$$e_x = \frac{M_y}{N} = \frac{107}{212.5} = 0.50 \text{ m}$$

$$X_{int.} = 2.32 \text{ m}$$

$$Y_{int.} = \frac{i_x^2}{e_y}$$

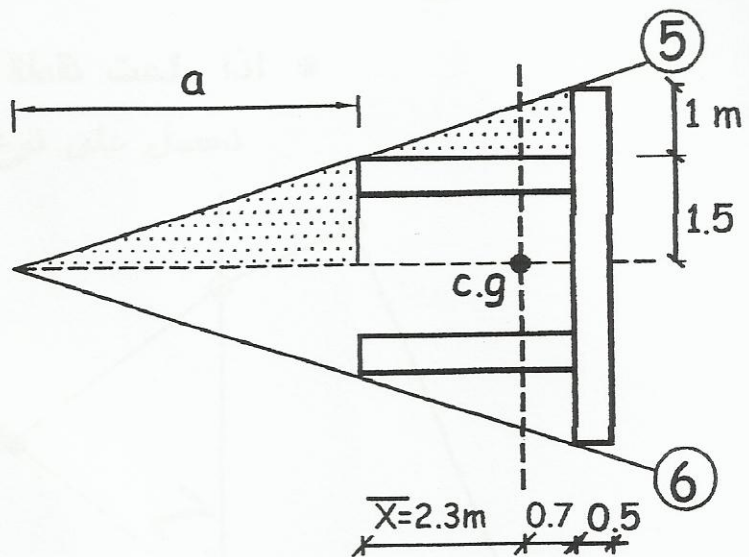
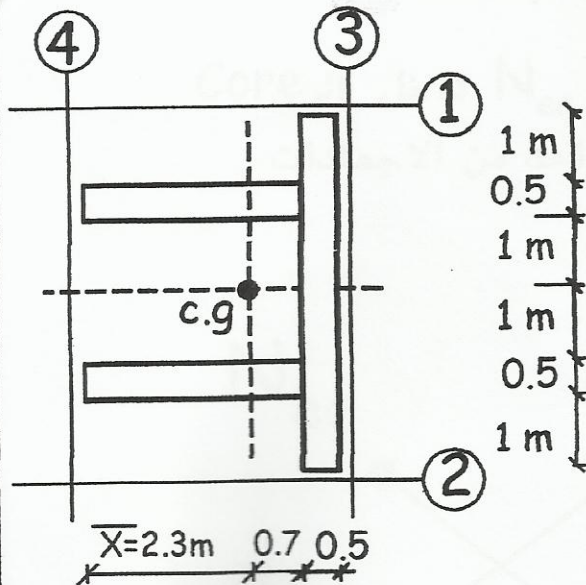
$$i_x^2 = \frac{I_x}{A} = \frac{9.95}{5.5} = 1.81 \text{ m}^2$$

$$e_y = \frac{M_x}{N} = \frac{132}{212.5} = 0.62 \text{ m}$$

$$Y_{int.} = 2.91 \text{ m}$$

$$i_x^2 = \frac{I_x}{A} = 1.81 \text{ m}^2$$

$$i_y^2 = \frac{I_y}{A} = 1.176 \text{ m}^2$$



NA (1)&(2):  $Y_{int.} = 2.5 \text{ m}$

$$\Rightarrow e_y = \frac{i_x^2}{Y_{int}} = \frac{1.81}{2.5} = 0.72 \text{ m}$$

NA (3):  $X_{int.} = 1.2 \text{ m}$

$$\Rightarrow e_x = \frac{i_y^2}{X_{int}} = \frac{1.176}{1.2} = 0.98 \text{ m}$$

NA (4):  $X_{int.} = 2.3 \text{ m}$

$$\Rightarrow e_x = \frac{i_y^2}{X_{int}} = \frac{1.176}{2.3} = 0.51 \text{ m}$$

NA (5): by similarity :

$$\frac{1.5}{a} = \frac{1}{3} = \frac{Y_{int}}{X_{int}} \Rightarrow a = 4.5 \text{ m}$$

$$\Rightarrow X_{int} = \bar{X} + a = 2.3 + 4.5 = 6.8 \text{ m} \Rightarrow e_x = \frac{i_y^2}{X_{int}} = \frac{1.176}{6.8} = 0.173 \text{ m}$$

$$\Rightarrow Y_{int} = 2.26 \text{ m} \Rightarrow e_y = \frac{i_x^2}{Y_{int}} = \frac{1.81}{2.26} = 0.798 \text{ m}$$

$$e_x = \frac{My}{N} = \frac{132}{212.5} = 0.62 \text{ m}$$

$$e_y = \frac{Mx}{N} = \frac{107}{212.5} = 0.5 \text{ m}$$

$$N_{eq} = N = 212.5 \text{ comp.}$$

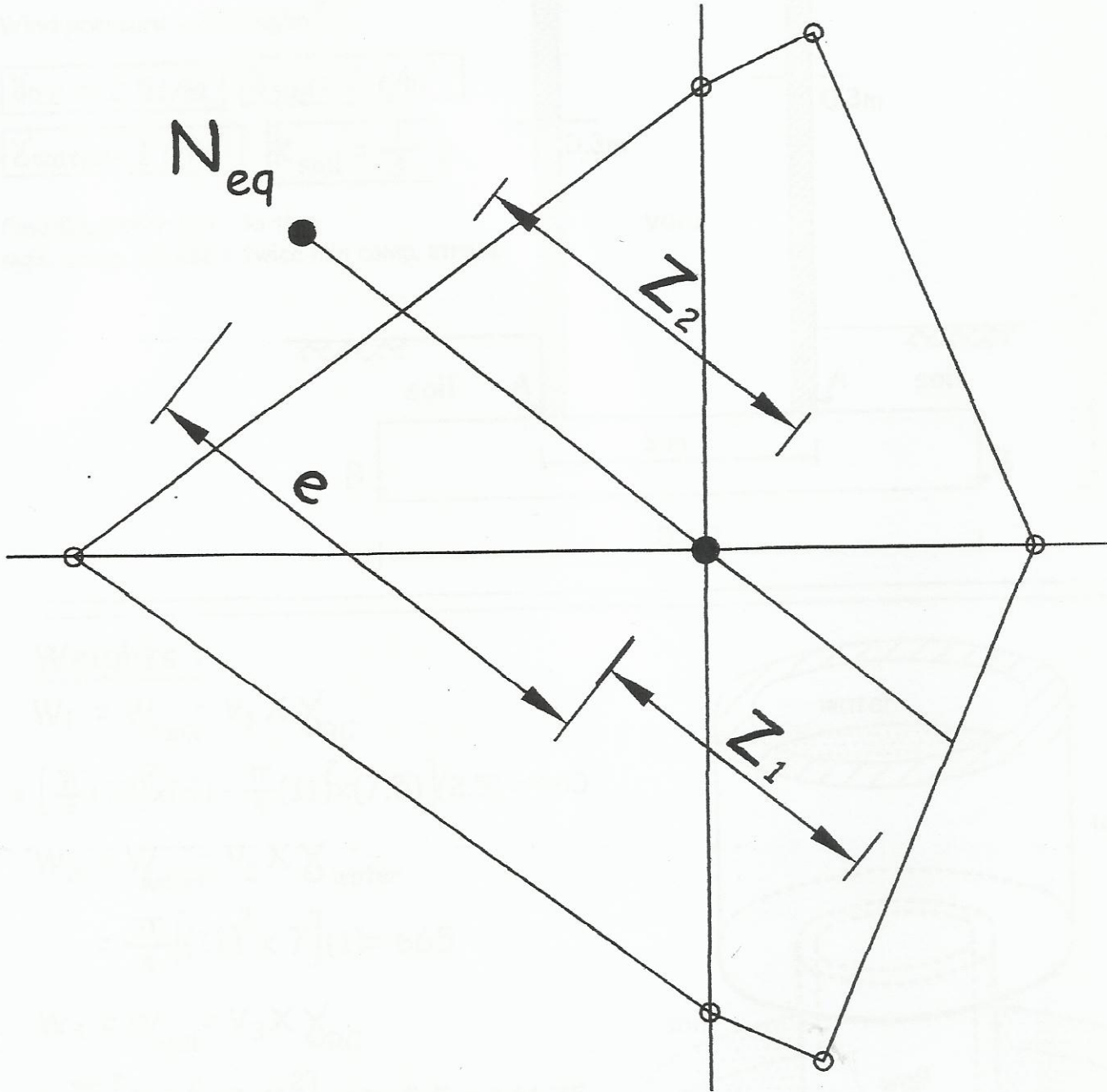


ملاحظة هامة جدا جدا • اذا وقعت نقطة الـ  $N_{eq}$  خارج الـ Core

نحصل على نوعين اجهادات

• اذا وقعت نقطة الـ  $N_{eq}$  داخل الـ Core

نحصل على نوع واحد من الاجهادات



$$f_1 = \frac{N}{A} \left[ \frac{Z_1 + e}{Z_1} \right] = \frac{-212.5}{5.5} \left[ \frac{4.9 + 7.9}{4.9} \right] = -100 \text{ t/m}^2$$

$$f_2 = \frac{N}{A} \left[ \frac{Z_2 - e}{Z_2} \right] = \frac{-212.5}{5.5} \left[ \frac{6 - 7.9}{6} \right] = +12.23 \text{ t/m}^2$$

• يتم قياس المسافات  $(Z_2)$   $(Z_1)$   $(e)$  بالمسطرة

## Example

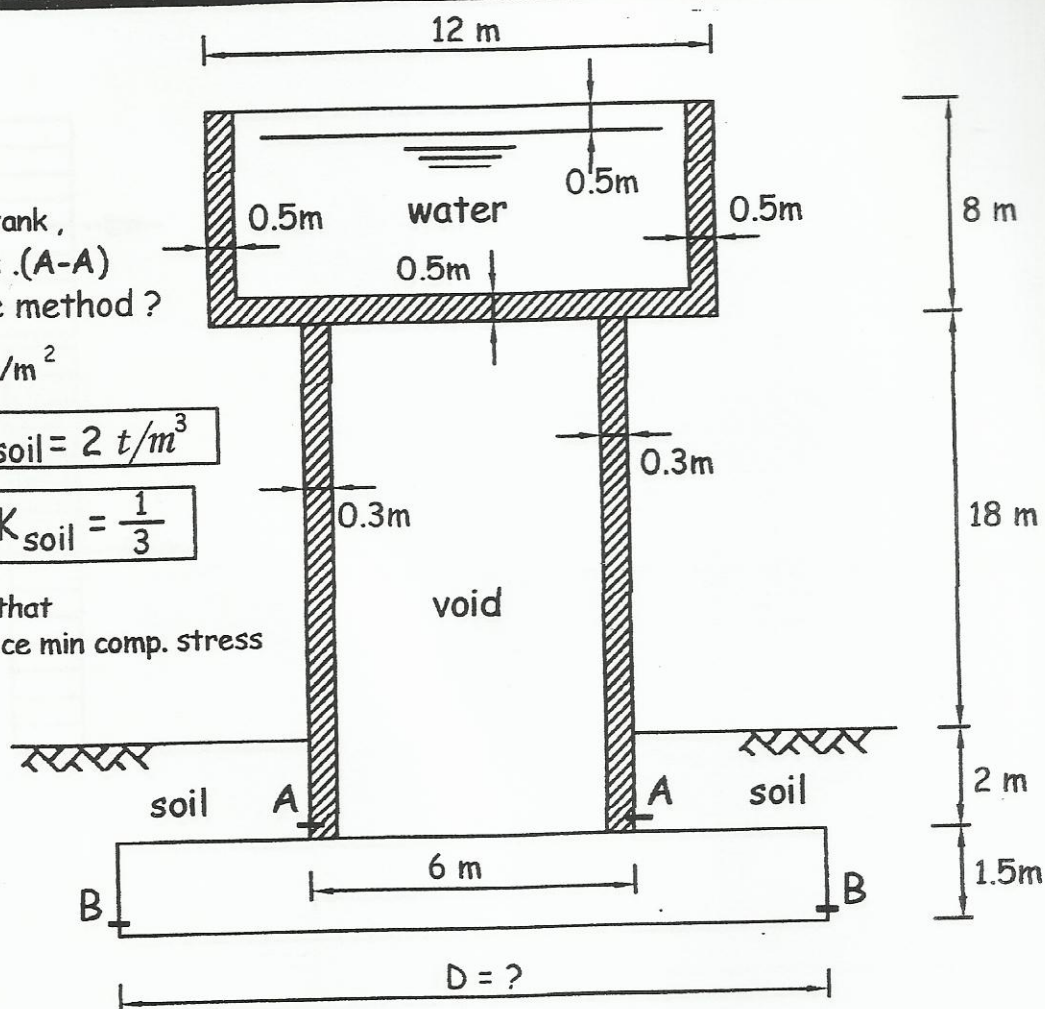
For the shown circular tank,  
Draw (N.S.D) for sec. (A-A)  
, then check by core method?

Wind pressure =  $200 \text{ kg/m}^2$

$$\gamma_{R.C} = 2.5 \text{ t/m}^3 \quad \gamma_{\text{soil}} = 2 \text{ t/m}^3$$

$$\gamma_{\text{water}} = 1 \text{ t/m}^3 \quad K_{\text{soil}} = \frac{1}{3}$$

Find Diameter (D), So that  
max. comp. stress = twice min comp. stress



### Weights :

$$W_1 = W_{\text{tank}} = V_1 \times \gamma_{RC}$$

$$= \left[ \frac{\pi}{4} (12)^2 \times (8) - \frac{\pi}{4} (11)^2 \times (7.5) \right] (2.5) = 480$$

$$W_2 = W_{\text{water}} = V_2 \times \gamma_{\text{water}}$$

$$= \frac{\pi}{4} [(11)^2 \times 7] (1) = 665$$

$$W_3 = W_{\text{wall}} = V_3 \times \gamma_{RC}$$

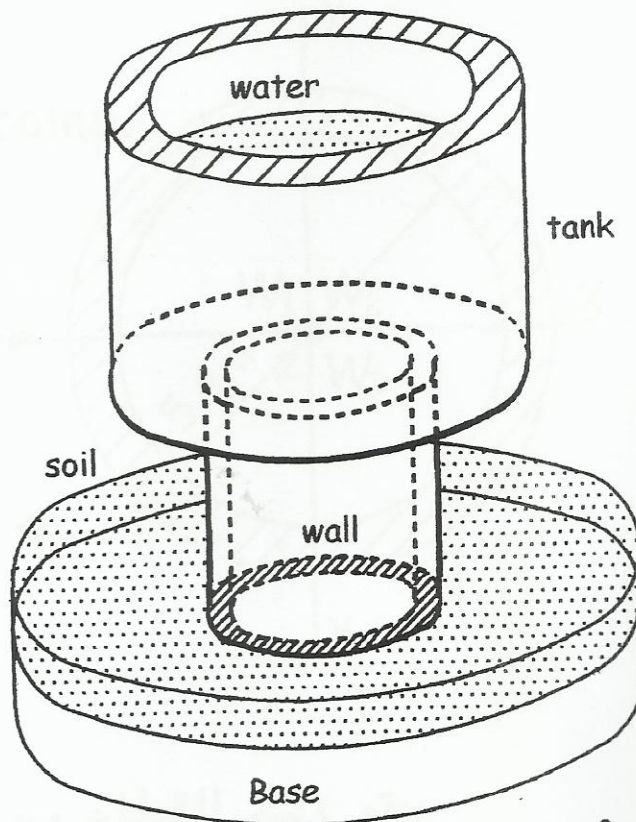
$$= \frac{\pi}{4} [(6)^2 - (5.4)^2] \times 18 \times 2.5 = 241.75$$

$$W_4 = W_{\text{soil}} = V_4 \times \gamma_{\text{soil}}$$

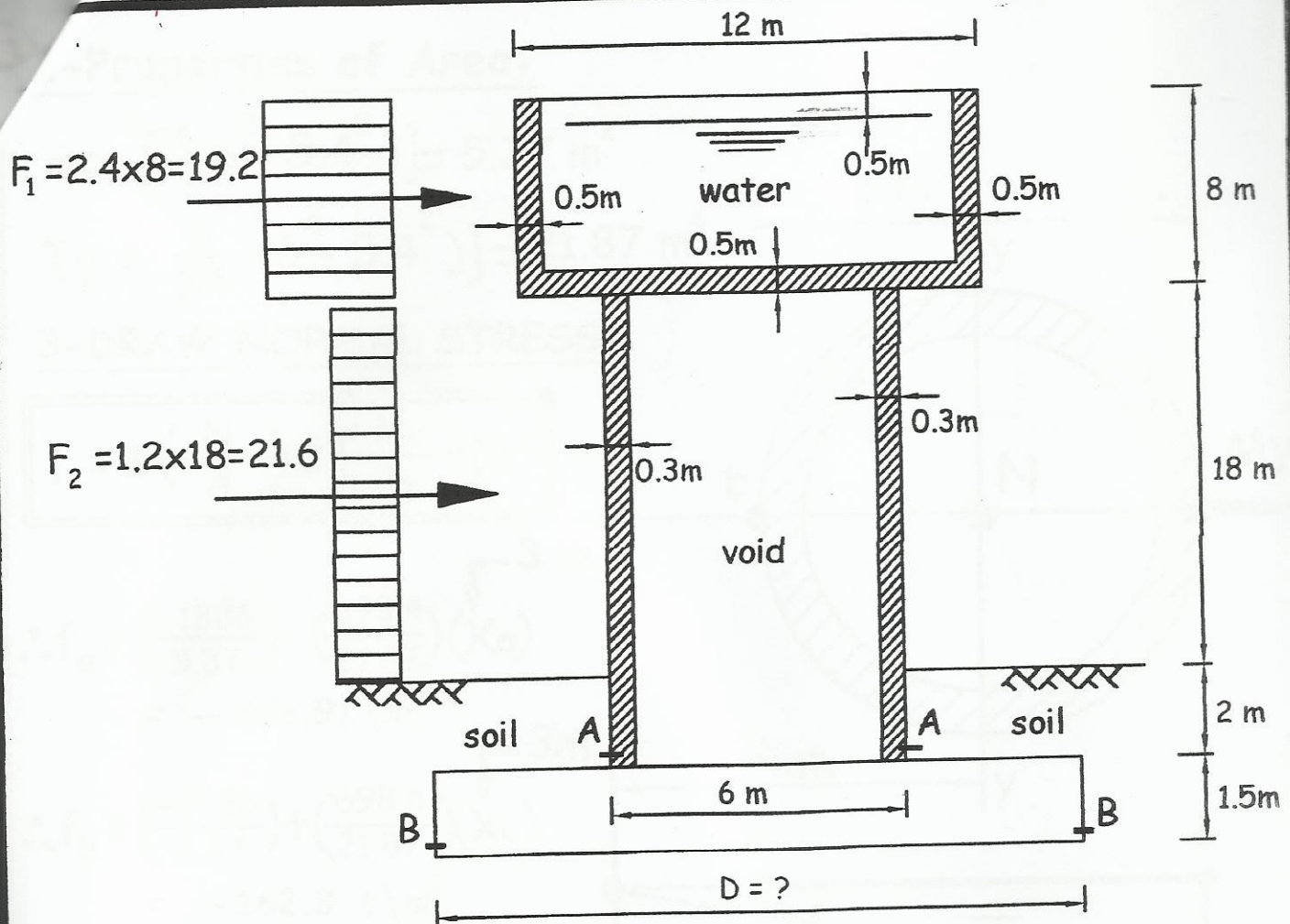
$$= \frac{\pi}{4} [(D)^2 - (6)^2] \times 2 \times 2 = 3.14 D^2 - 113$$

$$W_5 = W_{\text{base}} = V_5 \times \gamma$$

$$= \frac{\pi}{4} [(D)^2 \times 1.5] (2.5) = 2.945 D^2$$





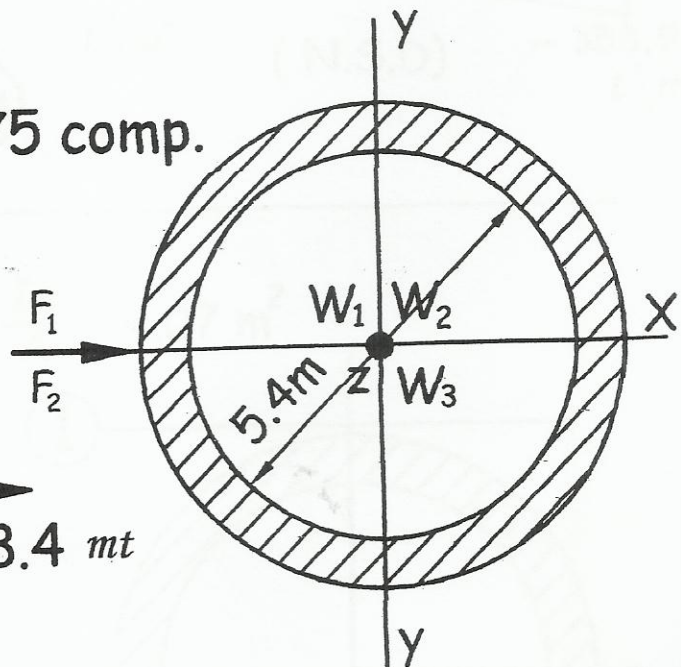


For section (A):

$$N = W_1 + W_2 + W_3 = 1386.75 \text{ comp.}$$

$$M_x = 0.0$$

$$M_y = 11 \times F_2 + 24 \times F_1 = 698.4 \text{ mt}$$



يتم رسم القطاع مع المحاور الخاصة به و اسقاط  
كل الاحمال الموجودة فوق منسوب القطاع

## 2-Properties of Area:

$$A = \frac{\pi}{4} [(6^2 - 5.4^2)] = 5.37 \text{ m}^2$$

$$I_y = \frac{\pi}{64} [(6^4 - 5.4^4)] = 21.87 \text{ m}^4$$

## 3-DRAW NORMAL STRESS:

$$f = \pm \left( \frac{N}{A} \right) \pm \left( \frac{M_y}{I_y} \right) (X)$$

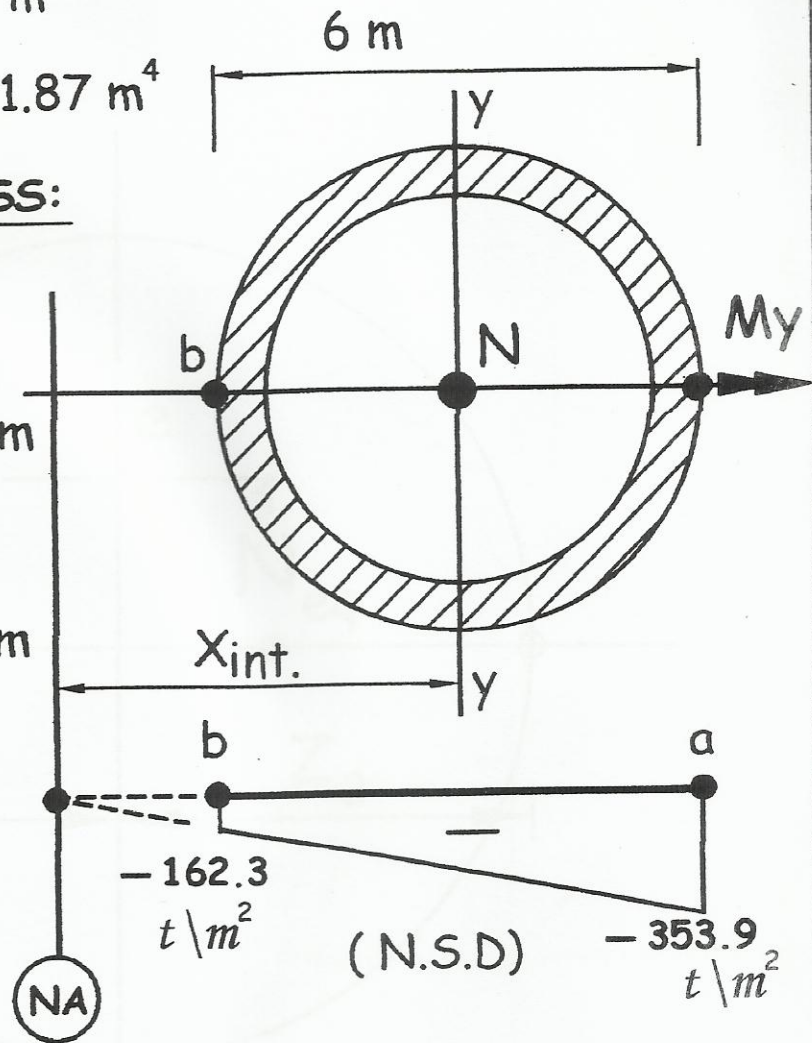
$$\therefore f_a = \left( \frac{-1386}{5.37} \right) - \left( \frac{698.4}{21.87} \right) (X_a)$$

$$= -353.9 \text{ t/m}^2$$

$$\therefore f_b = \left( \frac{-1386}{5.37} \right) + \left( \frac{698.4}{21.87} \right) (X_a)$$

$$= -162.3 \text{ t/m}^2$$

$$X_{\text{int.}} = \left| \frac{\left( \frac{1386}{5.37} \right)}{\left( \frac{698.4}{21.87} \right)} \right| = 8.08 \text{ m}$$



Check by Core :

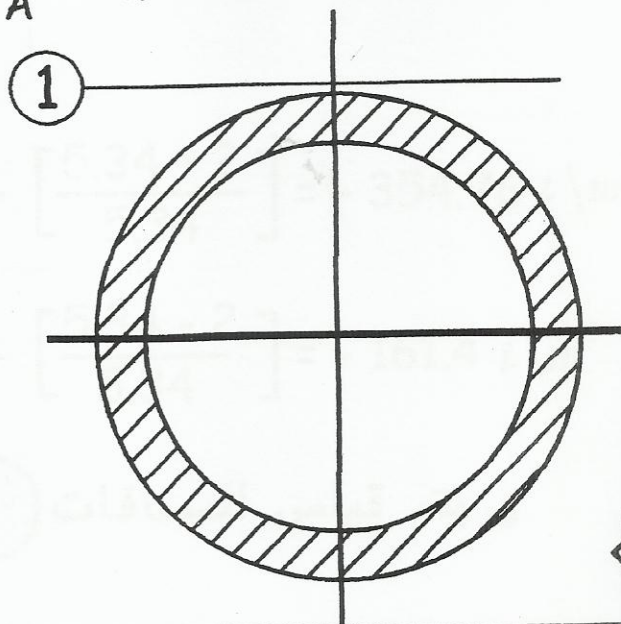
$$i_x^2 = i_y^2 = \frac{I_x}{A} = 4.07 \text{ m}^2$$

NA (1):

$$Y_{\text{int.}} = 3 \text{ m} \Rightarrow$$

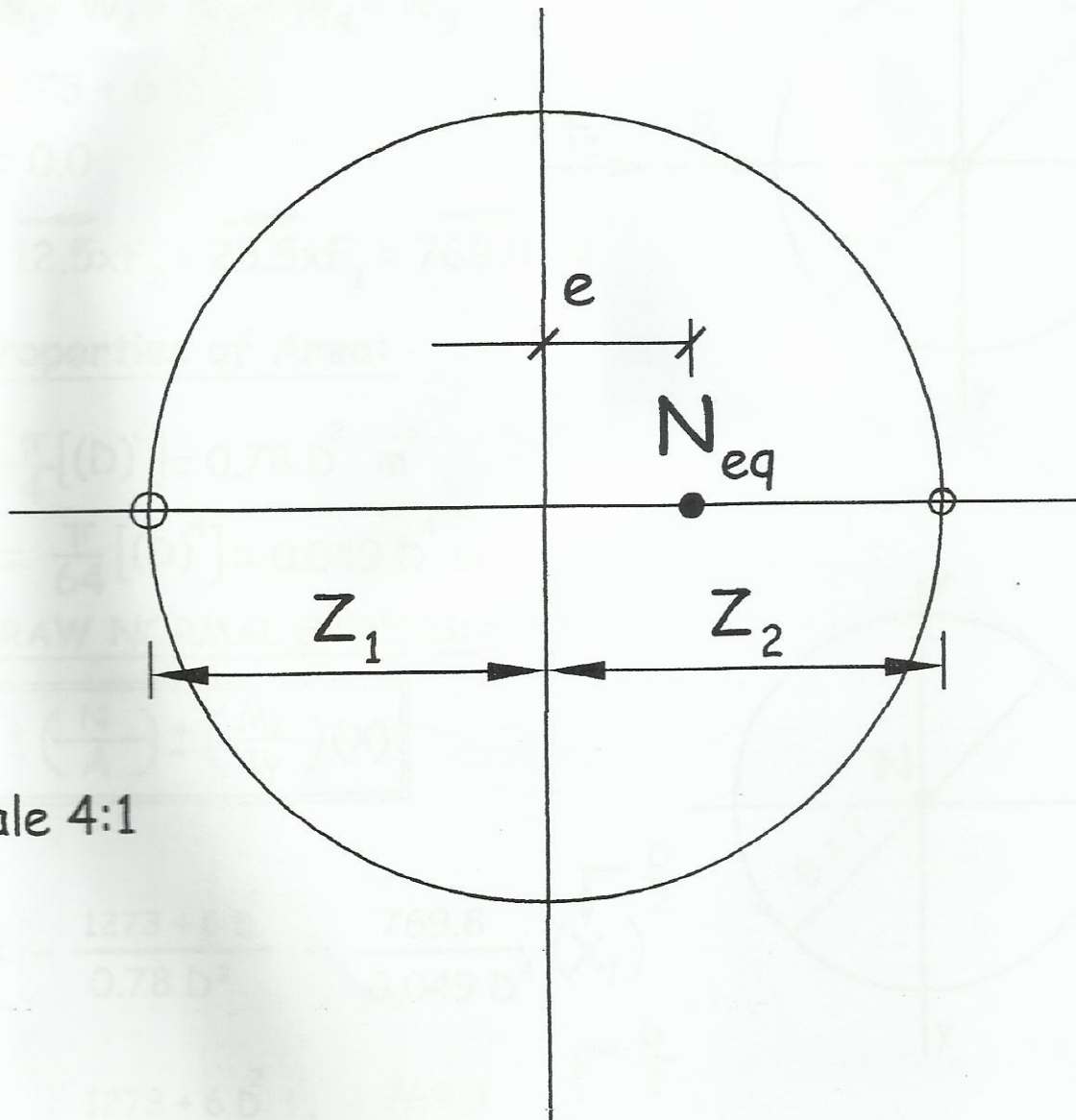
$$e_y = \frac{i_x^2}{Y_{\text{int}}} = \frac{4.07}{3} = 1.35 \text{ m}$$

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متماثلة حول جميع المحاور





$$e_x = \frac{My}{N_{eq}} = \frac{698.4}{1386} = 0.5 \text{ m}$$



Scale 4:1

$$f_1 = \frac{N}{A} \left[ \frac{Z_1 + e}{Z_1} \right] = \frac{-1386}{5.37} \left[ \frac{5.34 + 2}{5.34} \right] = -354.76 \text{ t/m}^2$$

$$f_2 = \frac{N}{A} \left[ \frac{Z_2 - e}{Z_2} \right] = \frac{-1386}{5.37} \left[ \frac{5.34 - 2}{5.34} \right] = -161.4 \text{ t/m}^2$$

• يتم قياس المسافات  $(Z_2)$   $(Z_1)$   $(e)$  بالمسطرة

• يتم رسم القطاع مع المحاور الخاصة به و اسقاط الموجودة فوق منسوب القطاع

For section (B):

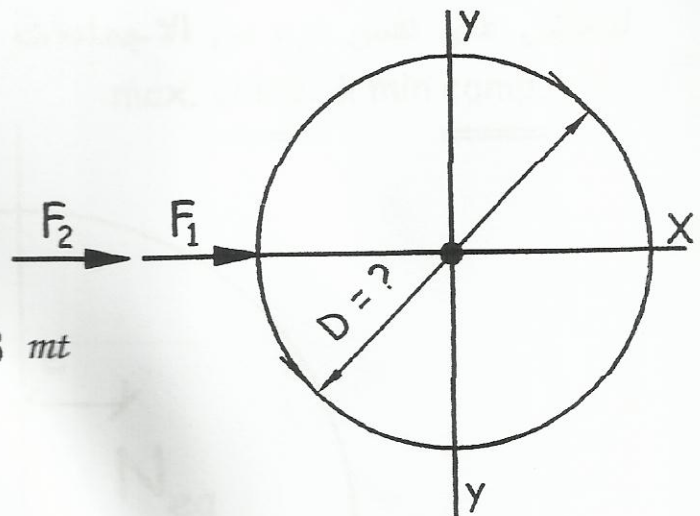
### 1-Straining actions

$$N = W_1 + W_2 + W_3 + W_4 + W_5$$

$$N = 1273 + 6 D^2$$

$$M_x = 0.0$$

$$M_y = 12.5 \times F_2 + 25.5 \times F_1 = 769.8 \text{ mt}$$



### 2-Properties of Area:

$$A = \frac{\pi}{4} [(D)^2] = 0.78 D^2 \text{ m}^2$$

$$I_y = \frac{\pi}{64} [(D)^4] = 0.049 D^4 \text{ m}^4$$

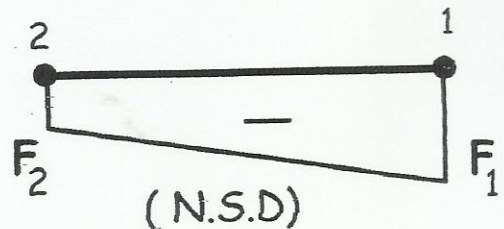
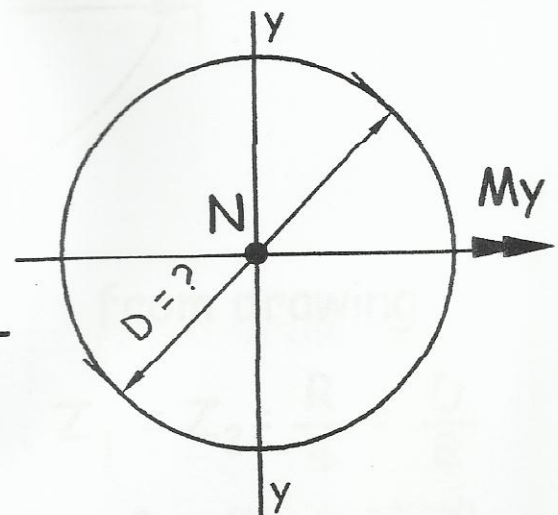
### 3-DRAW NORMAL STRESS:

$$f = \pm \left( \frac{N}{A} \right) \pm \left( \frac{M_y}{I_y} \right) (X)$$

$$\therefore f_1 = - \frac{1273 + 6 D^2}{0.78 D^2} - \frac{769.8}{0.049 D^4} \left( X_1 \right)^{\frac{D}{2}}$$

$$\therefore f_2 = - \frac{1273 + 6 D^2}{0.78 D^2} + \frac{769.8}{0.049 D^4} \left( X_2 \right)^{\frac{D}{2}}$$

But ,  $f_1 = 2 f_2$  Given



$$- \frac{1273 + 6 D^2}{0.78 D^2} - \frac{769.8}{0.049 D^4} \left( \frac{D}{2} \right) = 2 \left[ - \frac{1273 + 6 D^2}{0.78 D^2} + \frac{769.8}{0.049 D^4} \left( \frac{D}{2} \right) \right]$$

Get

$$D = 9.88 \text{ m}$$

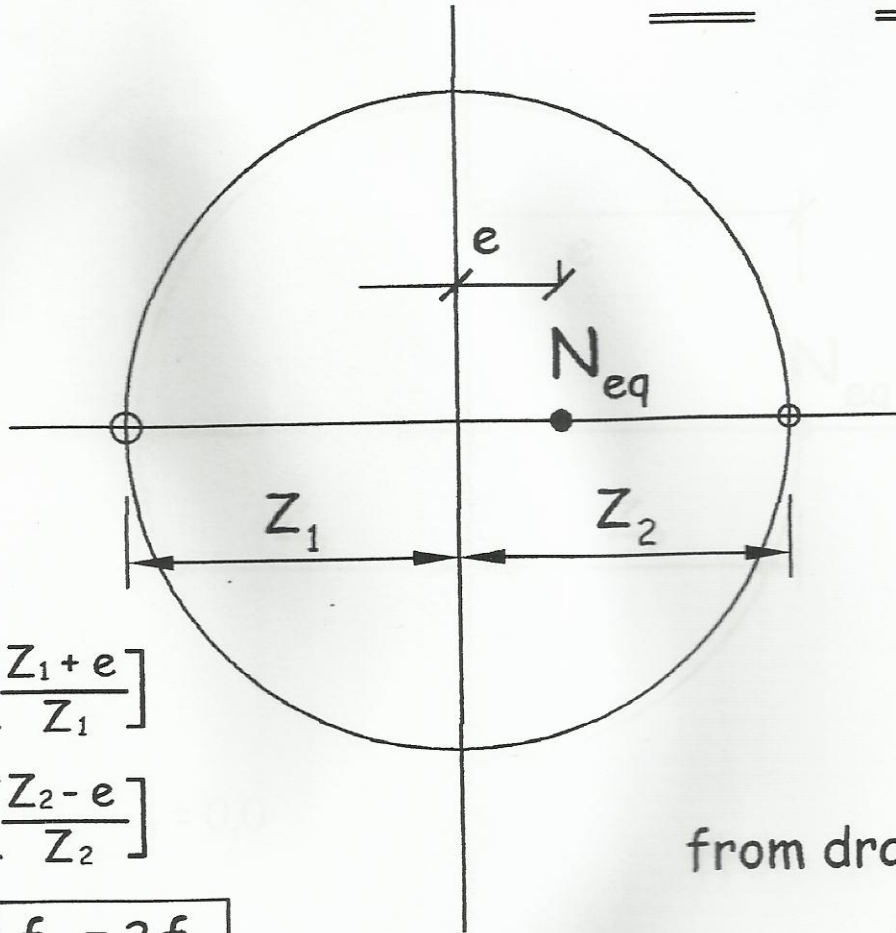


Get (D) by Core method :

ملاحظة هامة جدا جدا

$$\Rightarrow e_x = \frac{My}{N_{eq}} = \frac{769.8}{1273 + 6 D^2}$$

• يجب أن تقع الـ  $N_{eq}$  داخل الـ Core  
لنحصل على نفس نوع من الاجهادات  
max. comp. & min comp.



$$f_1 = \frac{N}{A} \left[ \frac{Z_1 + e}{Z_1} \right]$$

$$f_2 = \frac{N}{A} \left[ \frac{Z_2 - e}{Z_2} \right]$$

But ,  $f_1 = 2 f_2$

$$\frac{N}{A} \left[ \frac{Z_1 + e}{Z_1} \right] = (2) \frac{N}{A} \left[ \frac{Z_2 - e}{Z_2} \right]$$

$$\cancel{\frac{N}{A}} \left[ \frac{Z_1 + e}{\cancel{Z_1}} \right] = (2) \cancel{\frac{N}{A}} \left[ \frac{Z_2 - e}{\cancel{Z_2}} \right]$$

$$Z_1 + e = (2) [Z_2 - e]$$

$$\Rightarrow 3e = Z \Rightarrow 3 \left[ \frac{769.8}{1273 + 6 D^2} \right] = \frac{D}{8}$$

$$\Rightarrow \boxed{D = 9.88 \text{ m}}$$

from drawing

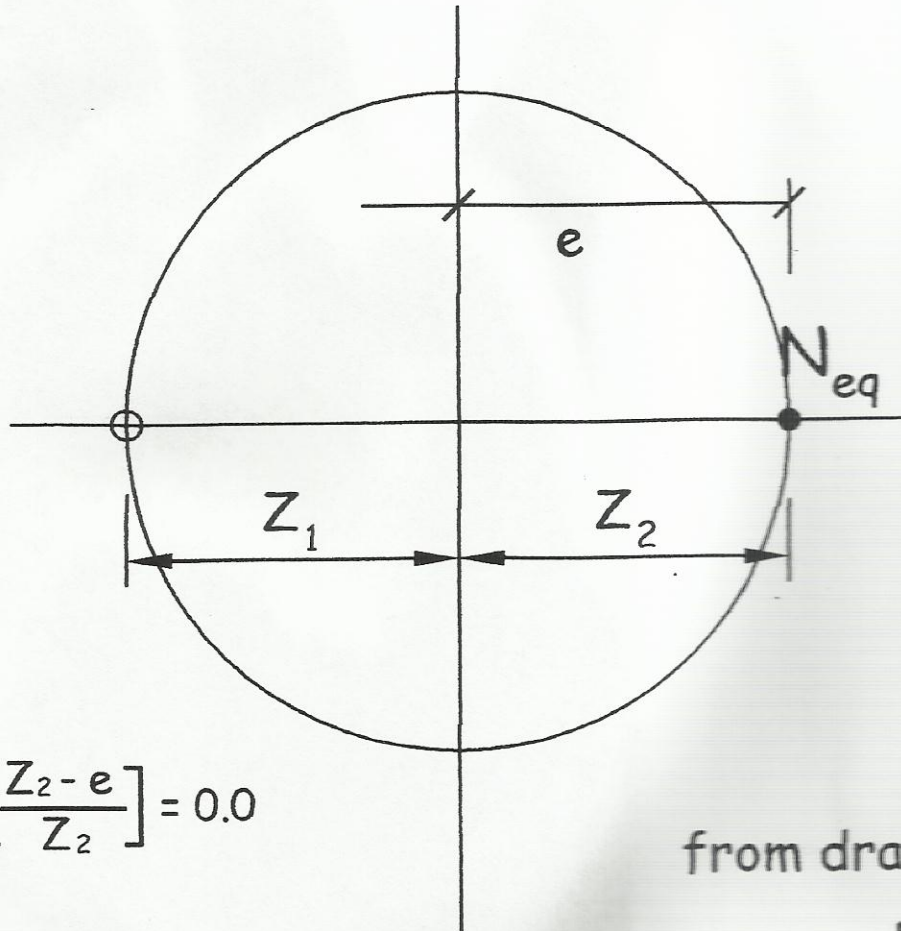
$$Z_1 = Z_2 = \frac{R}{4} = \frac{D}{8}$$

الاثبات في (9) Page

$$f_2 = \frac{N}{A} \left[ \frac{Z_2 - e}{Z_2} \right] = 0.0$$

• المطلوب الـ D بحيث No tension stress

والـ  $N_{eq}$  موجودة على مسار الـ Core



$$f_2 = \frac{N}{A} \left[ \frac{Z_2 - e}{Z_2} \right] = 0.0$$

$$Z_2 - e = 0.0$$

$$Z_2 = e$$

$$\frac{D}{8} = \left[ \frac{769.8}{1273 + 6 D^2} \right]$$

$$\Rightarrow \boxed{D = 4.43 \text{ m}}$$

from drawing

$$Z_1 = Z_2 = \frac{R}{4} = \frac{D}{8}$$

الاثبات في (9) Page